

An Efficient Key Assignment Scheme for Access Control in a Large Leaf Class Hierarchy

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Abstract

The employees of an organization are usually divided into different security classes to authorize the information retrieval, and the number of leaf classes is substantially larger than the number of non-leaf classes. Additionally, the alternations in leaf classes are more frequent than in non-leaf classes. We proposed a new key assignment scheme for controlling the access right in a large POSET (partially ordered set) hierarchy to reduce the required computation for key generation and

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derivation with the storage amount of data decreased.

Keywords: Access control, cryptography, data security, hierarchy, key management.

1 Introduction

The access control of resources in a social organization is getting more and more attention in recent years. In most social organizations, such as companies, governments and militaries, the employees are divided into different security classes according to their positions and access authorities [3, 6, 7, 14, 15, 17, 19, 22, 29, 30]. The access control privilege is assigned into different privileged classes as a user tree-structure. In the structure of privileged classes, the users in the higher security classes can access the data in the lower security classes but not vice versa. Usually, the number and the frequency of alternation of bottom classes (leaf nodes) are much larger than the number of non-bottom classes (non-leaf nodes) in a user tree-structure. We need a very efficient scheme to handle the access control problem for this type of user structure.

Under such a user hierarchy, the entities including people, work and other items are organized into a number of disjointed sets of security classes [1]. Assigning users to a security class is called “security clearance”. Let C_1, C_2, \dots, C_n be n disjointed security classes according to the significant levels and C is a partially ordered set (POSET) under a binary relation denoted by “ \leq ” where $C = \{C_1, C_2, \dots, C_n\}$. Note that $C_i \leq C_j$ means that the privilege in C_j is equal to or higher than the one in C_i where $C_i \in C$ and $C_j \in C$. Figure 1 shows a typical case of a POSET in a user hierarchy. For example, $C_2 \leq C_1$ means that C_1 is a predecessor of C_2 and C_2 is a successor of C_1 . If there is no C_k satisfying the relationship $C_2 \leq C_k \leq C_1$, then C_1 is called an immediate predecessor of C_2 and C_2 is an immediate successor of C_1 .

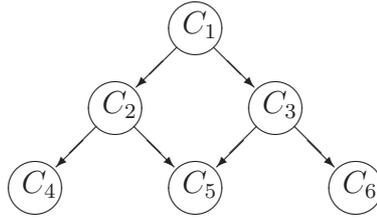


Figure 1: The POSET in a user hierarchy

1.1 Relative Works

Akl-Taylor first proposed a scheme for access control with a POSET hierarchy in 1983 [1]. The central authority (CA) assigns every security class C_i a public parameter PB_i and a secret key K_i . C_i can encrypt any plaintext with K_i by symmetric cryptosystem [12, 13], and C_j can retrieve the plaintext by the secret key which can be calculated from PB_i , PB_j and K_j when $C_i \leq C_j$. In the Akl-Taylor scheme, the access control problem is easily solved by a POSET hierarchy, but their scheme has some drawbacks. A large amount of storage is required to keep the public parameters when the user hierarchy is large, and all the keys in the system have to be redistributed when a new security class is added. In 1985, Mackinnon et al. proposed an improved scheme called “canonical assignment scheme”, which reduced the number of distinct primes in a user hierarchy [18]. Although this scheme can reduce the number of distinct primes, it still needs a large amount of storage and an optimal algorithm, which is not easy to find, for a complex or arbitrary user hierarchy.

Sandhu proposed a cryptographic implementation of a tree hierarchy in 1988 [20]. This method uses a one-way function and children’s identities to generate the secret keys without the extra public parameters. Unfortunately, Sandhu’s scheme could not provide a solution for the general case in a POSET hierarchy.

Harn and Lin proposed a new key assignment scheme with a bottom-up

key generation scheme in 1990 [8]. The security of Harn-Lin's scheme is based on the complexity of factoring out a big number. With this bottom-up key generation method, the storage space of public parameters is noticeably reduced. However, Harn-Lin's scheme still requires a large amount of storage space for a large user hierarchy [9].

In 1998, Yeh et al. proposed a key assignment scheme with a matrix model which is called "YCN scheme" [26]. By employing a derivation key and an encrypted data key, their scheme can prevent the illegal access and allow only the authorized classes to derive the encrypted key. However, Hwang pointed out that several classes can easily collaborate to derive the two keys in a special case [10, 16]. Later, in 2003, Yeh et al. proposed an improved scheme to fix the collusive attack problem [27].

Tzeng proposed a time-bound cryptographic key assignment scheme in a partially ordered hierarchy in 2002 [23]. The cryptographic keys of security classes are different in distinct periods. Each user can use the legal key during the authorized period only. When the time has expired, the user in the security class can not access any data of the descendent classes. However, Yi and Ye showed that Tzeng's scheme is insecure because any three users can collaborate to obtain the secret keys of some classes [28].

Hwang and Yang proposed an efficient access control scheme for those large partially ordered hierarchies in 2003 [11]. Hwang-Yang's scheme is based on both Akl-Taylor's and Harn-Lin's schemes with the mathematical concepts of combination to reduce the number of selected prime numbers and to support a dynamic POSET hierarchy. However, the leaf group is difficult to form in a general application and Hwang-Yang's scheme is insecure against the collusion attack [24].

Yang and Li proposed an efficient access control using one-way hash functions in 2004 [25]. When a class is eliminated from the hierarchy, the order of

the sibling would become a problem. Chen and Huang proposed a very efficient key management scheme for dynamic access control in 2005 [4]. Atallah et al. also proposed a pretty efficient access control scheme in 2005, but their scheme is not suitable for a deep tree or a tree with complex relationships [2]. Santis et al. proposed a time-bound and hierarchical key assignment scheme in 2006 [21] and Chung et al. proposed an access control scheme based on elliptic curve cryptosystem in 2008 [5]. However, all of the above schemes are not suitable for a large leaf class hierarchy.

1.2 Requirement of a Large Leaf Class Hierarchy

Most studies are designed for a general tree structure instead of a large leaf tree structure. The solution scheme should possess the following requirements.

1. The smallest space for storing the public parameters.
2. The guarantee of computation security.
3. The better efficiency of alternation occurring in lower-level classes.
4. Minimum influence on the whole structure when adding or deleting a class.

The number of prime numbers directly affects the space of the storage and causes the problem of computing load. Therefore, we have carefully considered that the amount of prime numbers used in the system should be reduced and proposed an efficient scheme for the dynamic key management.

1.3 Organization

This article is constructed as follows. The introduction is stated in Section 1. In Section 2, the efficient key assignment scheme for access control is proposed. The security and comparisons among schemes are discussed in Section 3. The last section is our conclusion.

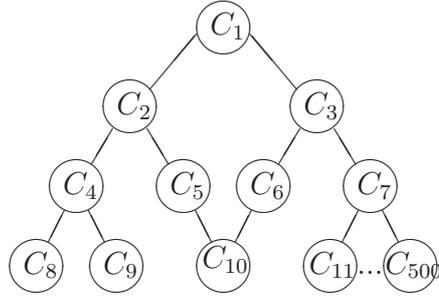


Figure 2: A POSET hierarchical structure

2 The Proposed Scheme

Basically, the number of the selected prime numbers in the system affects the storage space of data, the key generation time and key derivation time. Our scheme has a relatively small amount of the prime numbers.

2.1 Key Generation Phase

In the key generation phase, there is a CA in the system, and the security classes have the authorized relationships shown in Figure 2. The CA executes the following steps:

- Step 1. CA chooses two large primes p and q , and then computes the public parameter $m = p \cdot q$, where p and q must be kept in secret.
- Step 2. CA generates a random number K_0 where the K_0 and m are relative primes, and the condition $2 < K_0 < (m - 1)$ should be satisfied.
- Step 3. For every class C_i , which is a non-leaf security class or a leaf security class with two or more immediate ancestors in the hierarchy, CA selects a prime number e_i and computes the corresponding multiplicative inverse d_i to satisfy $d_i = e_i^{-1} \text{ mod } \phi(m)$, and then assigns the pair (e_i, d_i) to C_i .
- Step 4. For every leaf security class C_i , which has only one immediate ancestor in the hierarchy, CA randomly generates a secret key K_i and calculates a public parameter $PB_i = K_i \oplus H(K_j, C_i, C_j)$, where $H(\cdot)$ denotes a one-way function and C_j is the immediate

ancestor of C_i .

For every class C_k , which is a non-leaf security class or a leaf security class with two or more immediate ancestors in the hierarchy, CA calculates a secret key $K_k = K_0^{(d_k \cdot \prod_{all\ C_t} d_t \text{ mod } \phi(m))} \text{ mod } m$ and a public parameter $PB_k = e_k \cdot \prod_{all\ C_t} e_t$, where (e_t, d_t) is the key pair given by CA for the class C_t . Here, C_t is the successor of C_k and C_t is not a leaf class with one predecessor.

Step 5. CA passes the secret key K_i to every class C_i through a secure channel individually and publishes all public parameters and authorized relationships.

2.2 Key Derivation Phase

Assume that C_i and C_j are in the POSET hierarchy with relationship $C_i \leq C_j$, where C_i is an immediate successor of C_j . K_i and K_j are the secret keys of C_i and C_j , respectively. When a user u_j is assigned to C_j , u_j can derive the key K_i in C_i from the following formula:

$$K_i = \begin{cases} PB_i \oplus H(K_j, C_i, C_j) & \text{if } C_i \text{ is a leaf class with only} \\ & \text{one immediate ancestor } C_j. \\ PB_i \oplus H(K_j^{PB_j/PB_k}, C_i, C_j) & \text{if } C_i \text{ is a leaf class with only} \\ & \text{one immediate ancestor } C_k \\ & \text{where } C_i \leq C_k \leq C_j. \\ K_j^{(PB_j/PB_i)} \text{ mod } m & \text{otherwise} \end{cases}$$

Without knowing the $\phi(m)$, the user u_j in C_j can efficiently deduce the secret key K_i of C_i with its secret key K_j and the public parameters, PB_i and PB_j .

Theorem 1. *For two secure classes C_i and C_j with relationship $C_i \leq C_j$, C_j can derive the secret key K_i of C_i from the above formula.*

Proof. We have the public information (C_1, \dots, C_n) , (PB_1, \dots, PB_n) and one-way hash function $H(\cdot)$ in an n node hierarchy.

(1) C_i is a leaf class with only one predecessor.

- a. C_j is the immediate predecessor of C_i . It is trivial to get the key from the equation $K_i = PB_i \oplus H(K_j, C_i, C_j)$.
- b. There is a C_k to satisfy the relationship of $C_i \leq C_k \leq C_j$ where C_k is the immediate predecessor of C_i . Because we do not know the secret key K_k , we shall process the following steps. The C_t is a subset of C_j and C_t does not include the leaf class with only one immediate predecessor.

$$\begin{aligned}
K_i &= PB_i \oplus H(K_k, C_i, C_k) \\
&= PB_i \oplus H(K_0^{(d_k \bmod \phi(m))} \bmod m, C_i, C_k) \\
&= PB_i \oplus H(K_0^{((d_j \cdot \prod_{all\ C_t} d_t)(e_j \cdot \prod_{all\ C_t} e_t/e_k) \bmod \phi(m))} \bmod m, C_i, C_k) \\
&= PB_i \oplus H(K_j^{((e_j \cdot \prod_{all\ C_t} e_t/e_k) \bmod \phi(m))} \bmod m, C_i, C_k) \\
&= PB_i \oplus H(K_j^{PB_j/PB_k} \bmod m, C_i, C_k)
\end{aligned}$$

(2) C_i is a non-leaf class or a leaf class with multiple predecessors.

The C_t is a subset of C_j which does not include the leaf class with only one immediate predecessor, and the C_r is a subset of C_i and does not include the leaf class with only one immediate predecessor.

$$\begin{aligned}
K_i &= K_0^{(d_i \cdot \prod_{all\ C_r} d_r \bmod \phi(m))} \bmod m \\
&= K_0^{((d_j \cdot \prod_{all\ C_t} d_t)(e_j \cdot \prod_{all\ C_t} e_t/(e_i \cdot \prod_{all\ C_r} e_r) \bmod \phi(m))} \bmod m \\
&= K_j^{((e_j \cdot \prod_{all\ C_t} e_t/(e_i \cdot \prod_{all\ C_r} e_r)) \bmod \phi(m))} \bmod m \\
&= K_j^{PB_j/PB_i} \bmod m
\end{aligned}$$

□

2.3 Examples of Key Derivation

Assume that five hundred security classes (C_1, C_2, \dots, C_{500}) are in the POSET hierarchy structured shown in Figure 2. Table 1 shows how the secret keys and public parameters are assigned in our proposed method.

Table 1: An example of using the proposed scheme

Security classes (C_i)	Public parameters (PB_i)	Secret keys (K_i)
C_1	$e_1 e_2 e_3 e_4 e_5 e_6 e_7 e_{10}$	$K_0^{d_1 d_2 d_3 d_4 d_5 d_6 d_7 d_{10} \text{ mod } \phi(m)} \text{ mod } m$
C_2	$e_2 e_4 e_5 e_{10}$	$K_0^{d_2 d_4 d_5 d_{10} \text{ mod } \phi(m)} \text{ mod } m$
C_3	$e_3 e_6 e_7 e_{10}$	$K_0^{d_3 d_6 d_7 d_{10} \text{ mod } \phi(m)} \text{ mod } m$
C_4	e_4	$K_0^{d_4} \text{ mod } m$
C_5	$e_5 e_{10}$	$K_0^{d_5 d_{10} \text{ mod } \phi(m)} \text{ mod } m$
C_6	$e_6 e_{10}$	$K_0^{d_6 d_{10} \text{ mod } \phi(m)} \text{ mod } m$
C_7	e_7	$K_0^{d_7} \text{ mod } m$
C_8	$K_8 \oplus H(K_4, C_8, C_4)$	K_8
C_9	$K_9 \oplus H(K_4, C_8, C_4)$	K_9
C_{10}	e_{10}	$K_0^{d_{10}} \text{ mod } m$
C_{11}	$K_{11} \oplus H(K_7, C_{11}, C_7)$	K_{11}
\vdots	\vdots	\vdots
C_{500}	$K_{500} \oplus H(K_7, C_{500}, C_7)$	K_{500}

Case 1: *Deriving the key of a leaf class which has only one immediate predecessor*

A user u_1 in C_1 wishes to access information of user u_{500} in C_{500} , where $C_{500} \leq C_1$. The user u_1 can derive K_{500} with its secret key K_1 and the public parameter of the immediate predecessor of user u_{500} .

$$\begin{aligned}
 K_{500} &= PB_{500} \oplus H(K_7, C_{500}, C_7) \\
 &= PB_{500} \oplus H(K_1^{PB_1/PB_7} \text{ mod } m, C_{500}, C_7)
 \end{aligned}$$

The proof is stated as follows.

$$\begin{aligned}
K_{500} &= K_{500} \oplus H(K_7, C_{500}, C_7) \oplus H(K_7, C_{500}, C_7) \\
&= PB_{500} \oplus H(K_7, C_{500}, C_7) \\
&= PB_{500} \oplus H(K_0^{d_7} \text{ mod } m, C_{500}, C_7) \\
&= PB_{500} \oplus H((K_0^{d_1 d_2 d_3 d_4 d_5 d_6 d_7})^{e_1 e_2 e_3 e_4 e_5 e_6 e_7} \text{ mod } m, C_{500}, C_7) \\
&= PB_{500} \oplus H((K_1)^{e_1 e_2 e_3 e_4 e_5 e_6 e_7 e_{10}/e_7} \text{ mod } m, C_{500}, C_7) \\
&= PB_{500} \oplus H(K_1^{PB_1/PB_7} \text{ mod } m, C_{500}, C_7)
\end{aligned}$$

Case 2: *Deriving the key of a non-leaf successor or the key of a leaf class which has more than one immediate predecessor*

A user u_1 in C_1 wishes to access the information of user u_{10} in C_{10} , where $C_{10} \leq C_1$. The user u_1 can derive K_{10} with its secret key K_1 , its public parameter PB_1 and the public parameter of the user u_{10} .

$$K_{10} = K_1^{PB_1/PB_{10}} \text{ mod } m$$

The proof is stated as follows.

$$\begin{aligned}
K_{10} &= K_0^{d_{10}} \text{ mod } m \\
&= K_0^{(d_{10} d_1 d_2 d_3 d_4 d_5 d_6 d_7)(e_1 e_2 e_3 e_4 e_5 e_6 e_7)} \text{ mod } m \\
&= K_1^{(e_1 e_2 e_3 e_4 e_5 e_6 e_7)} \text{ mod } m \\
&= K_1^{(e_{10} e_1 e_2 e_3 e_4 e_5 e_6 e_7)/e_{10}} \text{ mod } m \\
&= K_1^{PB_1/PB_{10}} \text{ mod } m
\end{aligned}$$

2.4 Dynamic Key Management

In a realistic environment, a key assignment scheme must have the dynamic management ability for adding and deleting security classes.

2.4.1 Adding a security class

When adding a new class, the condition being considered is to check if the new class is a leaf class and whether it has only one immediate predecessor.

Adding a class with only one immediate predecessor

When adding a leaf class C_n under one security class C_r . CA only assigns a random secret key K_n and computes a public parameter PB_n to C_n from Step 4 of the key generation phase. Almost all ancestors of the new security class C_n are unaffected. For example, let us add a new class C_{502} under the class C_7 in Figure 2. CA assigns a random secret key K_{501} and a public parameter $PB_{501} = K_{501} \oplus H(K_7, C_{501}, C_7)$ to C_{501} . While other 500 classes do not change their secret keys and public parameters.

Only if the new immediate predecessor class is a leaf class before the new class C_n is added, then its predecessors should be updated. In this case, the CA needs to assign a pair (e_n, d_n) to C_n and to recompute the public parameters and secret keys of all ancestors along the path to the root class. For example, let us add a new class C_{502} under the class C_{500} in Figure 2. CA assigns a (e_{500}, d_{500}) to class C_{500} and recomputes the $PB_{500} = e_{500}$ and $K_{500} = K_0^{d_0} \text{ mod } m$. Then CA chooses a random secret key K_{502} to C_{502} and computes the public parameter $PB_{502} = K_{502} \oplus H(K_{500}, C_{502}, C_{500})$, plus the predecessors of C_{500} should be updated as shown in Table 2 while other 496 classes remain unchanged.

Table 2: The new data for predecessors of the new adding class C_{500}

Class	Secret Key	Public parameter
C_7	$K_7 = K_0^{d_7 d_{500} \text{ mod } \phi(m)} \text{ mod } m$	$PB_7 = e_7 e_{500}$
C_3	$K_3 = K_0^{d_3 d_6 d_7 d_{10} d_{500} \text{ mod } \phi(m)} \text{ mod } m$	$PB_3 = e_3 e_6 e_7 e_{10} e_{500}$
C_1	$K_1 = K_0^{d_1 d_2 d_3 d_4 d_5 d_6 d_7 d_{10} d_{500} \text{ mod } \phi(m)} \text{ mod } m$	$PB_1 = e_1 e_2 e_3 e_4 e_5 e_6 e_7 e_{10} e_{500}$

Adding a class with multiple immediate predecessors

When a new security class C_n is added under two or more immediate ances-

tors or C_n is a non-leaf class, CA assigns a pair (e_n, d_n) to C_n and computes the K_n with the formula in Step 4 of the key generation phase. Next, CA computes the public parameter PB_n by multiplying the new prime e_n with the value of e given by CA of all descendants of C_n except the leaf class with one predecessor. Along the path to the root, CA modifies the public parameters and secret keys of the ancestors of C_n with the steps in the key generation phase. In this case, only the classes along the path from C_n to root should be recomputed to their public parameters and secret keys. Most descendants are still not affected unless the new class is added above a leaf class, and then the leaf class should be recomputed with the public parameter. For example, let us add a new class C_{503} under the classes C_4 and C_5 in Figure 2. CA assigns key pair (e_{503}, d_{503}) to class C_{503} and generates the secret key $K_{503} = K_0^{d_{503}} \text{ mod } m$ and a public parameter $PB_{503} = e_{503}$ for C_{503} . Next, CA regenerates the secret keys and public parameters by Step 4 of the key generation phase for new ancestor classes, C_4 , C_5 , C_2 and C_1 while other 496 classes remain unchanged.

2.4.2 Cancelling a security class

When removing a security class, the condition being considered is to check whether the class is a leaf class with only one immediate predecessor.

Removing a class with only one immediate predecessor

CA simply voids the public parameter and secret key of the removed class while eliminating the class, and almost all classes are not affected. For example, let us remove the class C_8 in Figure 2. CA eliminates PB_8 and K_8 and all 499 public parameters and secret keys of the system remain unchanged.

If the immediate successor becomes a leaf class after the cancelling process is completed, CA chooses a random secret key for the new leaf class and computes the public parameter for the class, as described in the key generation phase. Let us remove the class C_9 following the above example. CA eliminates

PB_9 and K_9 and deletes the class C_9 . Next, CA selects a new random secret key K_4 for C_4 and computes the public parameter $PB_4 = K_4 \oplus H(K_2, C_4, C_2)$ because C_4 is now a leaf class. Also, the secret keys and public parameters of classes C_2 and C_1 should be recomputed while other 495 public parameters and 499 secret keys of the classes in the system remain unchanged.

Removing a non-leaf class

When removing a non-leaf class, CA voids the public parameter and the secret key of the eliminated class when deleting the security class. Then, CA reorganizes the structure and recomputes the public parameters and secret keys for all ancestors of the eliminated class, and most of the successors are not affected. For example, let us remove the class C_2 in Figure 2. CA eliminates PB_2 and K_2 and deletes the class C_2 from the system structure then a new structure is organized. Class C_4 and class C_5 become the immediate successors of the class C_1 . Therefore, K_1 and PB_1 are recomputed while other 498 public parameters and secret keys of the system remain unchanged.

If the immediate successor of the eliminated class is a leaf class, the class should be recomputed after the cancelling process has been done. For example, let us remove the class C_4 in Figure 2. CA either keeps the old secret keys of the class C_8 and class C_9 , or regenerates new secret keys for C_8 and C_9 , and the CA recomputes the public parameters $PB_8 = K_8 \oplus H(K_2, C_8, C_2)$ and $PB_9 = K_9 \oplus H(K_2, C_9, C_2)$ because the new immediate predecessor is class C_2 while other 496 public parameters and secret keys of the system remain unchanged.

Removing a leaf class with multiple immediate predecessors

When removing a leaf class with multiple immediate predecessors, CA voids the public parameter of the eliminated class and the secret key of the class

while deleting the security class. Then, CA recomputes the public parameters and secret keys for all ancestors of the eliminated class along the path to the root class, and most of the successors are not affected. However, if the immediate successor is a leaf class after the cancelling process is finished, most of the successors would be affected. For example, let us remove the class C_{10} in Figure 2. CA eliminates PB_{10} and K_{10} when deleting the class C_{10} from the system. Then CA recomputes or regenerates the secret keys and public parameters of the classes C_5 , C_6 , C_3 , C_2 , and C_1 . Note that C_5 and C_6 only became leaf classes after C_{10} is removed, so they should each be assigned a new secret key and a new public parameter. Other 494 public parameters and secret keys of the classes in the system remain unchanged.

3 Security and Efficiency Comparison

In this section, we will present the security analysis of the proposed scheme in a large leaf class hierarchy. Also, we will examine the required storage and computational complexity.

3.1 Security Analysis

The security analysis of our proposed scheme in possible attacks is described as follows.

1. Modular m attack:

Any adversary can easily obtain public parameters e_i and the modular m , but he could not mathematically prove that the multiplicative inverse d_i can be derived from the known e_i and m . Basically, the security of our scheme is similar to that of RSA cryptosystem, where its security is based on the difficulty of factoring m into m 's two prime factors. Many factorizing methods are similar to the brute-force attack which would further result in time-consuming efforts. Hence, by using the current

factoring algorithms, it would be inefficient to factor a product of two large primes, especially the strong primes.

2. Contrary attack:

Assume that there are C_i and C_j in a POSET hierarchy and $C_i \leq C_j$. C_j could easily deduce the secret key K_i in C_i using the key derivation method, but not vice versa. If a user in C_i wants to derive the secret key K_j in C_j with his K_i and public parameters, the key K_j could not be obtained because its security is based on the difficulties of factorization and the one-way function inverse. No user is capable of deriving the secret key of his predecessor or other unauthorized classes from the public parameters.

3. Common modulus attack:

When a plaintext m is being encrypted twice using (e_1, d_1, n) and (e_2, d_2, n) with a common modulus n , m can be deduced if e_1 and e_2 are relative primes. By the extension of Euclidean algorithm, v_1 and v_2 are existent such that the equation $v_1e_1 + v_2e_2 = 1$ holds. Assume that the two ciphertexts are $c_1 = m^{e_1} \bmod n$ and $c_2 = m^{e_2} \bmod n$, the plaintext m can be obtained by the computation of $m = c_1^{v_1} \times c_2^{v_2} \bmod n$. Nevertheless, anyone who obtains the public parameters (e_i, n) and common modulus n still could not affect the security of our scheme since d_i and K_0 are being secretly kept by CA. Even though each security class uses the same modulus with different exponential parameters, our scheme is proven to be secured against the common modulus attack.

4. Collaborative attack:

Two or more users in the lower security classes may want to collaboratively derive the secret key of the higher class C_j with mutual information. The users of lower levels can collect the public parameters and

their secret keys, but $K_j = K_0^{\prod d_i} \text{ mod } m$ is only known by CA and C_j . Without K_0 , it is impossible to derive the secret key for unauthorized classes in the collaborative attack.

3.2 Efficiency Comparisons

In this subsection, the comparisons among Akl-Taylor’s scheme, Harn-Lin’s scheme, Hwang-Yang’s scheme, and our scheme are presented because all of them are suited for a large leaf class structure. All the schemes need an online CA to keep all the public parameters PB_i . Table 3 shows four items: number of primes, maximum public parameter, the complexity of key generation, and key derivation.

Table 3: The comparisons of space and computational complexity ($z \leq y \leq n$)

Schemes	Number of primes	Maximum public parameter	Key generation	Key derivation
Akl-Taylor	n	$\prod_{i=1}^n e_i$	$O(n)$	$O(1)$
Harn-Lin	n	$\prod_{i=1}^n e_i$	$O(n)$	$O(1)$
Hwang-Yang	y	$\prod_{i=1}^y e_i$	$O(y)$	$O(1)$
Our	z	$\prod_{i=1}^z e_i$	$O(z)$	$O(1)$

The generation of prime number will bring issues to the storage size and computing power so we will discuss it first. In the procedure of deciding prime number, let’s assume a POSET hierarchy has n security classes. In Akl-Taylor’s scheme and Harn-Lin’s scheme, both of them choose a prime number for each class so the number is correlated to the total number of nodes n .

The number of the primes in Hwang-Yang’s scheme should be computed by the formula:

$$y = \left(\sum_{\text{for all } LG_i} g_i \right) + n_a + n_t, \quad (1)$$

where:

- LG is the term for “leaf-group”, where the security classes are the leaf secure classes, and LG_i denotes the i th leaf-group.

- g_i is a minimum number such that $\binom{g_i}{k} \geq h_i$. $\binom{g_i}{k}$, the result of mathematical combination, is a number of ways for choosing k from g_i and h_i denotes the number of classes in LG_i . Here, the k is the number of primes for distinguishing leaf classes in a leaf group.
- n_a denotes the number of leaf security classes that have two or more immediate ancestors.
- n_t denotes the number of non-leaf security classes.

Our scheme is based on the Hwang-Yang's scheme with a large improvement. The number of the primes in our scheme is computed by the formula:

$$z = n_a + n_t \quad (2)$$

where n_a and n_t are defined as in Hwang-Yang's scheme.

Theorem 2. *In a n node hierarchy tree, the number of primes used in Akl-Taylor's scheme, Harn-Lin's scheme, Hwang-Yang's scheme, and our proposed scheme are n , n , y and z respectively. The condition $z \leq y \leq n$ should be satisfied.*

Proof. The number of primes used in Akl-Taylor's scheme and Harn-Lin's scheme are the same as the total number of nodes, so both schemes need n prime numbers. From Equation (1) and Equation (2), the condition $z \leq y$ is achieved. So every leaf class that has more than one immediate predecessor is the worst case of z , and the upper limit of z is n . Therefore, the condition $z \leq y \leq n$ is satisfied. Of course, the worst case for all schemes is that they all need n prime numbers. \square

Assume that there is a large hierarchy which has 500 security classes shown in Figure 2. Both Akl-Taylor's and Harn-Lin's schemes must have $n = 500$ primes, so the amount of required storage is enormous for a large hierarchy.

In Hwang-Yang's scheme, $LG_1 = \{C_8, C_9\}$, $LG_2 = \{C_{10}\}$ and $LG_3 = \{C_{11}, \dots, C_{500}\}$ so it reduces the number of primes to $y = (2 + 1 + 12) + 1 + 7 = 23$ primes (with Equation (1)) by the mathematical concept of combination). In the same environment, our proposed scheme only needs $z = 1 + 7 = 8$ primes with the Equation (2). By comparing the required number of primes, our scheme is substantially lower than other schemes since $8 \leq 23 \leq 500$.

The length of the maximum number of public parameters results in the computational load of CA. It costs n multiplications in both Akl-Taylor's and Harn-Lin's schemes when the maximum number of public parameters is being computed. There are y multiplications in Hwang-Yang's scheme and z multiplications in our scheme. For example, in the case of Figure 2, there are 500 security classes in the POSET structure. We first calculated the number of primes to be used for each class by using the above schemes in Table 4. From the results, the maximum multiplications used for every scheme are 499 times in Akl-Taylor's scheme, 500 times in Har-Lin's scheme, 23 times in Hwang-Yang's scheme and 8 times in our scheme. Note that this data shows only the number for the most complex computational class obviously, our scheme is the most efficient one.

The computational complexity of the key generation is usually proportional to the number of primes. The computational complexity of our scheme is the most efficient comparing with other schemes, where $O(z) \leq O(y) \leq O(n)$ and the key derivation in all schemes is only $O(1)$ if the computation of the hash function is disregarded. Our scheme obviously executed more efficiently than other schemes from the compared results.

The storage space of secret key depends on the access method. Both Akl-Taylor's and Harn-Lin's schemes assign the public parameters directly, so that each class records its own key and its successors'. On the contrary, both Hwang-Yang's and our schemes utilize the key derivation method to obtain a

Table 4: Public parameters for each security class in different schemes

Scheme	Security classes	Public parameters (PBi)	Number of primes
Akl-Taylor's	C_1	1	1
	C_2	$e_1 e_3 e_6 e_7 e_{10} \cdots e_{500}$	495
	C_3	$e_2 e_4 e_5 e_8 e_{10}$	5
	\vdots	\vdots	\vdots
	C_8	$e_1 e_2 e_3 e_4 e_5 e_6 e_7 e_9 \cdots e_{500}$	499
	C_{500}	$e_1 \cdots e_{499}$	499
Har-Lin's	C_1	$e_1 \cdots e_{500}$	500
	C_2	$e_2 e_4 e_5 e_8 e_9 e_{10}$	6
	C_3	$e_3 e_6 e_7 e_{10} \cdots e_{500}$	494
	\vdots	\vdots	\vdots
	C_8	e_8	1
	C_{500}	e_{500}	1
Hwang-Yang's	C_1	$e_1 \cdots e_{23}$	23
	C_2	$e_2 e_4 e_5 e_8 e_9$	5
	C_3	$e_3 e_6 e_7 e_{10} e_{12} \cdots e_{23}$	16
	\vdots	\vdots	\vdots
	C_8	e_8	1
	C_{500}	$e_{20} e_{21} e_{22} e_{23}$	4
Our	C_1	$e_1 \cdots e_8$	8
	C_2	$e_2 e_4 e_5 e_8$	4
	C_3	$e_3 e_6 e_7 e_8$	4
	\vdots	\vdots	\vdots
	C_8	$K_8 \oplus H(K_4, C_8, C_4)$	0
	C_{500}	$K_{500} \oplus H(K_7, C_{500}, C_7)$	0

successor's key so that each class only records its secret key. For example, in the case shown in Figure 2, both Akl-Taylor's and Harn-Lin's schemes need storage space for 1991 keys where class C_1 records 500 keys, C_2 records 6 keys, C_3 records 494 keys, C_4 records 3 keys, C_5 and C_6 records 2 keys, C_7 records 491 keys, and all leaf classes record their own keys only. Both Hwang-Yang's and our schemes need space for 500 keys only. Let us assume each public parameter is 1024 bits, so both Akl-Taylor's and Harn-Lin's schemes need a size of 1991×1024 bits for secret key storage. Both Hwang-Yang's and our schemes only need a size of 500×1024 bits for key storage.

4 Conclusion

We have proposed a new key assignment to solve the problems of access control for a large POSET hierarchy. With substantially fewer numbers of primes and noticeable storage saving, the proposed scheme offers a worthy improvement in efficiency. Additionally, our scheme can also ensure that the security of the predecessor could not be revealed by any unauthorized successors from the violation of access policy. Moreover, our proposed scheme efficiently offers dynamic key management when a class is added or removed while satisfying the requirements listed in Section 1.2.

In an organization, the number of leaf classes is significantly larger than the number of non-leaf classes. The alternation in leaf classes happens more frequently than in non-leaf classes. Our proposed scheme offers a perfect reduction on the number of primes, which results in a notable efficiency improvement. When a class is added or removed, recomputing for all the parameters and keys of the organization became unnecessary. Our proposed scheme has the lowest amount of key regeneration when the leaf class is added or removed. Compared with other schemes, our proposed scheme has the highest efficiency and still maintains the essential and sufficient security in a large POSET hi-

erarchy.

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