

# A Coefficient of Variation Method to Measure the Extents of Decentralization for Bitcoin and Ethereum Networks

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(Received Nov. 20, 2018; Revised and Accepted Aug. 5, 2019; First Online Aug. 5, 2019)

## Abstract

The most primary advantage of Bitcoin and Ethereum systems is widely understood to be decentralization. However, despite the widely acknowledged importance of this property, most studies on this topic lack quantification, and none of them performs a measurement on the extent of decentralization they achieve in practice. In this paper, we present a coefficient of variation method in probability theory and statistics to quantify decentralization. Using the coefficient of variation, we calculate the dispersion extents of blocks mined and address balances to quantify the extents of decentralization for Bitcoin and Ethereum systems, and the results of calculations indicate that Bitcoin's mining is more approximately 27.3% decentralized than Ethereum with top 19 pool samples, and Bitcoin's wealth is more approximately 16.5% decentralized than Ethereum with 100 samples. Our method can be used to measure the extent of decentralization for any blockchain system.

*Keywords:* Bitcoin; Blockchain; Coefficient of Variation; Decentralization; Ethereum

## 1 Introduction

Bitcoin is a digital currency implementation based on blockchain technology that was invented by Satoshi Nakamoto in 2008 [14]. Bitcoin network is the first digital currency system that has been tested in large scale and long time in history. As a public blockchain platform, for adapting to more complex and flexible application scenarios, Ethereum [3] has further extended the functions of Bitcoin for digital currency transactions, supporting the important feature of smart contract. The common advantage of Bitcoin and Ethereum systems is widely understood to be decentralization that does not have any central authority or server and their networks are peer-to-peer. By storing data across its decentralized network,

the blockchain eliminates a number of risks that come with data being held centrally.

Since decentralization is the most important property in blockchain, many studies about the decentralization were proposed. Croman and Gencer *et al.* proposed the technical evaluation of blockchain decentralization systems, mainly focusing on the network congestion or delay to evaluate the performance of the blockchain distributed network [5, 8, 12, 16, 20]. They analyze how fundamental and circumstantial bottlenecks in Bitcoin limit the ability of its current peer-to-peer overlay network to support substantially higher throughputs and lower latencies. Their results suggest that reparameterization of block size and intervals should be viewed only as a first increment toward achieving next-generation, high-load blockchain protocols, and major advances will additionally require a basic rethinking of technical approaches. They offer a structured perspective on the design space for such approaches. Within this perspective, they enumerate and briefly discuss a number of recently proposed protocol ideas and offer several new ideas and open challenges.

Gervais *et al.* revealed that there are many important operations and decisions in Bitcoin system which is not decentralized, and they revealed that some nodes control services, decision-making, transactions and mining in Bitcoin system, finally they gave a way to optimize the decentralization of Bitcoin network [4, 9, 10, 13, 17]. They show that the vital operations and decisions that Bitcoin is currently undertaking are not decentralized. They also show that third-party entities can unilaterally decide to "devalue" any specific set of Bitcoin addresses pertaining to any entity participating in the system. Finally, they explore possible avenues to enhance the decentralization in the Bitcoin system. Ron and Shamir analyzed the transaction data of Bitcoin and revealed the occurrence of large transactions in the Bitcoin system at a certain point in time [11, 15, 18].

These existed research papers above are based on data

analysis of Bitcoin transaction behavior to illustrate the drawbacks of the low extent of decentralization in Bitcoin system. Although these studies are mainly concerned about the decentralization of blockchain, none of them performs a measurement on the extent of decentralization they achieve in practice. The closest research work to ours is the paper [19] that only focuses on evaluating a critical value of the number of nodes needed to control over 51% of the network by using a Nakamoto coefficient, rather than quantifying the dispersion of a set of data of blockchain systems, such as blocks mined and address balance and so on.

Herein, we must be able to measure the data dispersion extents of the targets of nodes in blockchain systems before we improve the decentralization. In this paper, we present a coefficient of variation method in probability theory and statistics to measure and quantify the extents of decentralization for blockchain systems. Using the coefficient of variation, we measure the dispersion extents of blocks mined and address balances to quantify the extents of decentralization for blockchain systems. The remainder of this paper is organized as follows. In section 2, we introduce the theory of the coefficient of variation in probability theory and statistics, and the meanings of decentralization in blockchain systems. In section 3, we propose a quantitative measurement method to measure the data dispersion extent based on the coefficient of variation, and in section 4, we calculate the dispersion extents of blocks mined and address balances by using the measurement method. In section 5, we compare the results of the coefficient of variation between Bitcoin and Ethereum systems. Finally, we conclude the paper in section 6.

## 2 Background

In this section, we first introduce the theory of the coefficient of variation in probability theory and statistics, and we illustrate the meanings of decentralization in blockchain systems to introduce the measurements of decentralization.

### 2.1 Coefficient of Variation

In probability theory and statistics, the coefficient of variation, also known as relative standard deviation, is a standardized measure of dispersion of a probability distribution or frequency distribution. The coefficient of variation ( $c_v$ ) is defined as the ratio of the standard deviation ( $\sigma$ ) to the mean ( $\mu$ ):  $c_v = \sigma/\mu$ . It shows the extent of variability in relation to the mean of the population. The coefficient of variation should be computed only for data measured on a ratio scale, as these are the measurements that allow the division operation.

The coefficient of variation is useful because the standard deviation of data must always be understood in the context of the mean of the data. In contrast, the actual value of the coefficient of variation is independent of the

unit in which the measurement has been taken, so it is a dimensionless number. For comparison between data sets with different units or widely different means, one should use the coefficient of variation instead of the standard deviation. The value of coefficient of variation is larger, the greater the degree of dispersion.

In this paper, we use the coefficient of variation to measure the extents of decentralization with dimensionless numbers for Bitcoin and Ethereum systems. We consider the extents with the two targets: blocks mined, and address balance.

### 2.2 Decentralization

Decentralization is the process by which the activities of an organization, particularly those regarding planning and decision making, are distributed or delegated away from a central, authoritative location or group.

In blockchain systems, the decentralization means that no single individual can destroy transactions in the network, and any transaction request requires the consensus of most participants. Bitcoin and Ethereum also have a peer-to-peer network for disseminating block and transaction information. Both Bitcoin and Ethereum also contain full nodes, which serve two critical roles: (1) to relay blocks and transactions to miners (2) and to answer queries for end users about the state of the blockchain. In the Bitcoin and Ethereum protocols, users submit transactions for miners to sequence into blocks. Better decentralization of miners means higher resistance against censorship of individual transactions. Specifically, a decentralized system (like Bitcoin or Ethereum) is composed of a set of decentralized subsystems (like mining, exchanges, nodes, developers, clients, and so on). Srinivasan *et al.* used these six subsystems to calculate a critical value with a Nakamoto coefficient, and to illustrate how many nodes needed to control over 51% of the network in Bitcoin or Ethereum [19].

In this paper, we will calculate the dispersion degrees by two targets (blocks mined and address balance) to measure the extents of decentralization for Bitcoin and Ethereum systems. Please note: you may decide to use different subsystems or targets based on which ones you consider essential to decentralization of the system as a whole.

## 3 Measurement Method

As mentioned above, we use the coefficient of variation to measure the dispersion degree for dimensionless data sets in Bitcoin and Ethereum systems. Herein, we elaborate the inferring process of coefficient of variation according to the variance and standard deviation, and then we present the formula of the coefficient of variation as a measurement method.

In probability theory and statistics, variance is the expectation of the squared deviation of a random variable

from its mean. Informally, it measures how far a set of (random) numbers are spread out from their average value. Variance is a central role in statistics, where some ideas that use it include descriptive statistics, statistical inference, hypothesis testing, and Monte Carlo sampling. Variance is an important tool, where statistical analysis of data is common. Variance is the square of the standard deviation, the second central moment of a distribution, and the covariance of the random variable with itself, and it is often represented by  $Var(X)$ . If the generator of random variable  $X$  is discrete with probability mass function  $x_1 \mapsto p_1, x_2 \mapsto p_2, \dots, x_n \mapsto p_n$  then

$$Var(X) = \sum_{i=1}^n p_i \cdot (x_i - \mu)^2,$$

where  $\mu$  is the expected value, i.e.  $\mu = \sum_{i=1}^n p_i x_i$ . When such a discrete weighted variance is specified by weights whose sum is not 1, one divides by the sum of the weights. Therefore, in statistics, the variance of a set of  $n$  equally likely values can be written as

$$Var(X) = \frac{1}{n} \sum_{i=1}^n (x_i - \mu)^2,$$

where  $\mu$  is the average value, i.e.  $\mu = \frac{1}{n} \sum_{i=1}^n x_i$ .

In statistics, the standard deviation (SD, also represented by the lower case Greek letter sigma  $\sigma$ ) is a measure that is used to quantify the amount of variation or dispersion of a set of data values. A low standard deviation indicates that the data points tend to be close to the mean (also called the expected value) of the set, while a high standard deviation indicates that the data points are spread out over a wider range of values. The standard deviation of a random variable, statistical population, data set, is the square root of its variance, i.e.,

$$\sigma = \sqrt{Var(X)} = \sqrt{\frac{1}{n} \sum_{i=1}^n (x_i - \mu)^2}$$

where  $\mu = \frac{1}{n} \sum_{i=1}^n x_i$ .

Coefficient of variation is another statistic to measure the degree of variation of observed values in data. When comparing the degree of variability of two or more data, the standard deviation can be used directly if the unit of measurement is the same as the average. If the unit and/or average are different, the standard deviation could not be used to compare the degree of variation, but the ratio of the standard deviation to the average (relative value) should be used to compare. The ratio of standard deviation to average is called coefficient of variation ( $c_v$ ), i.e.,

$$c_v = \frac{\sigma}{\mu}$$

where  $\sigma = \sqrt{\frac{1}{n} \sum_{i=1}^n (x_i - \mu)^2}$  and  $\mu = \frac{1}{n} \sum_{i=1}^n x_i$ . Coefficient of variation can eliminate the effect of unit and/or

average differences on the comparison of variability between two or more data sets. Therefore, coefficient of variation can be used to calculate the different dimensionless data sets between Bitcoin and Ethereum. More theories about variance, standard deviation, and coefficient of variation, please refer to the probability theory and statistics textbooks.

## 4 Calculations

According to the measurement method presented above, let's now calculate coefficients of variation for the blocks mined and address balance in Bitcoin and Ethereum networks. We can calculate the decentralized extents each of them according to coefficients of variation.

### 4.1 Blocks Mined

The quantity of blocks mined reflects the priority to account in blockchain networks. The data is more dispersed (or polarized), the ability of the miners controlling the entire blockchain network is more powerful, and the extent of decentralization of the blockchain network is lower. On the contrary, the data is more average, the ability of the miners controlling the entire blockchain network is weaker, and the extent of decentralization of the blockchain network is higher.

Hence, we use the coefficient of variation as the measurement method to calculate and quantify the degrees of data dispersion for Bitcoin and Ethereum networks, and we can compare the extents of decentralization between them.

#### 4.1.1 Coefficient of Variation of Bitcoin Blocks Mined

We catch the data of Bitcoin blocks mined over the last 7 days from the website [btc.com](http://btc.com) on Oct. 25, 2018, where Bitcoin's data will be updated in real time, as show in Figure 1.

The green frame in Figure 1 is the data top list of Bitcoin blocks mined. The data distribution of top 19 blocks mined in Bitcoin network is as show in Figure 2. We can see that the top 7 miners mined most blocks, and they can influence the decentralized extent of entire Bitcoin network.

According to the measurement method presented above, we use the random variable  $X = \{161, 136, 110, 101, 95, 90, 73, 16, 15, 15, 12, 11, 10, 10, 7, 6, 4, 2, 1\}$  and sample number  $n = 19$  to calculate the coefficient of

Pool	Hashrate Share	Hashrate	Blocks Mined	Empty Blocks Count	Empty Blocks Percentage	Avg. Block Size (Bytes)	Avg. Tx Fees Per Block (BTC)	Tx Fees % of Block Reward
1 BTC.com	16.65 %	8.20 EH/s	161	4	2.48 %	1,055,771	0.13199030	1.06 %
2 AntPool	14.06 %	6.93 EH/s	136	1	0.74 %	730,825	0.09653624	0.77 %
3 ViaBTC	11.38 %	5.60 EH/s	110	1	0.91 %	953,433	0.10927257	0.87 %
4 SlushPool	10.44 %	5.14 EH/s	101	1	0.99 %	974,467	0.11446046	0.92 %
5 BTC.TOP	9.82 %	4.84 EH/s	95	1	1.05 %	1,005,207	0.11535621	0.92 %
6 F2Pool	9.31 %	4.58 EH/s	90	0	0.00 %	1,062,745	0.12640051	1.01 %
7 Poolin	7.55 %	3.72 EH/s	73	1	1.37 %	1,069,483	0.12907499	1.03 %
8 Huobi.pool	1.65 %	814.82 PH/s	16	0	0.00 %	940,827	0.11471356	0.92 %
9 BitClub	1.55 %	763.89 PH/s	15	0	0.00 %	877,048	0.10521577	0.84 %
10 DPOOL	1.55 %	763.89 PH/s	15	0	0.00 %	959,886	0.17730335	1.42 %
11 BitFury	1.24 %	611.11 PH/s	12	0	0.00 %	683,110	0.12251172	0.98 %
12 Bixin	1.14 %	560.19 PH/s	11	0	0.00 %	1,000,779	0.07636004	0.61 %
13 58COIN	1.03 %	509.26 PH/s	10	0	0.00 %	633,567	0.05980556	0.48 %
14 WAYI.CN	1.03 %	509.26 PH/s	10	0	0.00 %	1,207,203	0.14989612	1.20 %
15 Bitcoin.com	0.72 %	356.48 PH/s	7	0	0.00 %	800,584	0.07289596	0.58 %
16 BWPool	0.62 %	305.56 PH/s	6	0	0.00 %	1,149,830	0.10385478	0.83 %
17 KanoPool	0.41 %	203.70 PH/s	4	0	0.00 %	992,993	0.19477824	1.56 %
18 BTPOOL	0.21 %	101.85 PH/s	2	0	0.00 %	1,125,270	0.08888516	0.71 %
19 CKPool	0.10 %	50.93 PH/s	1	0	0.00 %	831,358	0.09131175	0.73 %

Figure 1: Miner distribution sorted by blocks mined in Bitcoin network over the last 7 days (Data from <https://btc.com/> on Oct. 25, 2018 [1])

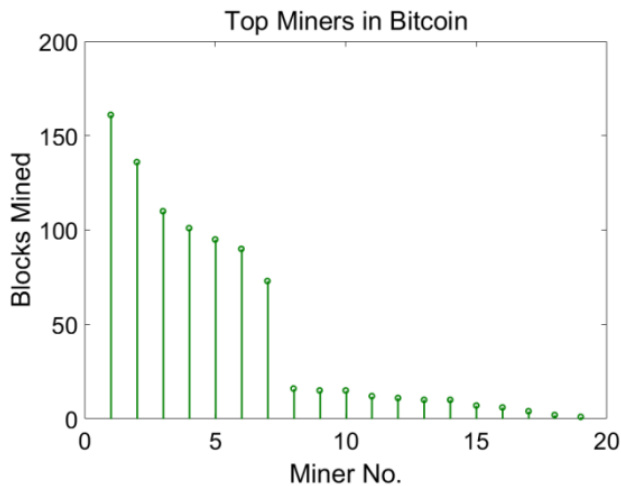


Figure 2: The distribution of top 19 blocks mined in Bitcoin network

variation that is introduced above as follows.

$$\mu = \frac{1}{n} \sum_{i=1}^n x_i \approx 46.05$$

$$\sigma = \sqrt{\frac{1}{n} \sum_{i=1}^n (x_i - \mu)^2} \approx 51.38$$

$$c_v = \frac{\sigma}{\mu} \approx 1.12.$$

We obtain the value of coefficient of variation of Bitcoin blocks mined is approximately equal to 1.12.

#### 4.1.2 Coefficient of Variation of Ethereum Blocks Mined

In the same way, we obtain the Ethereum block data over the last 7 days on Oct. 25, 2018 from the website ether-scan.io, where Ethereum’s data will be updated in real time, as show in Figure 3.

The red frame in Figure 3 is the data top list of Ethereum blocks mined. The data distribution of top 19 blocks mined in Ethereum network is as show in Figure 4. We can see that the only top 5 miners mined most blocks, and they can influence the decentralized extent of entire Ethereum network.

We also use the random variable  $Y = \{11389, 9569, 5711, 4334, 3748, 816, 729, 591, 589, 461, 378, 329, 315,$

Rank	Address	Blocks Mined	Percentage
1	0xea674fdde714fd979de3edf0f56aa9716b898ec8 (Ethernine)	11389	26.6073%
2	0x5a0b54d5dc17e0aad383d2db43b0a0d3e029c4c (SparkPool)	9569	22.3554%
3	0x829bd824b016326a401d083b3d092293333a830 (F2Pool_2)	5711	13.3422%
4	0x52bc44d5378309ee2abf1539b71de1b7d7be3b5 (Nanopool)	4334	10.1252%
5	0xb2930b35844a230f00e51431acae96fe543a0347 (MiningPoolHub_1)	3748	8.7562%
6	0x2a65aca4d5fc5b5c859090a6c34d164135398226 (DwarfPool_1)	816	1.9064%
7	0xd438323c8d1d8e0e03bdfab849871fa17e61807	729	1.7031%
8	0x52e44f279f4203dcf680395379e5f9990a69f13c (bw)	591	1.3807%
9	0x70aec4b9cfa7b55c0711b82dd719049d615e21d	589	1.3760%
10	0x2a5994b501e6a560e727b6c2de5d856396aadd38	461	1.0770%
11	0x35f61dfb08ada13eba64bf156b80d3d5b3a738d	378	0.8831%
12	0xcc16e3c00dbbe76603fa833ec20a48f786dfe610	329	0.7686%
13	0x09ab1303d3ccaf5f018cd511146b07a240c70294 (MinerallPool)	315	0.7359%
14	0x005e288d713a5fb3d7c9cf1b43810a98688c7223	301	0.7032%
15	0xb75d1e62b10e4ba91315c4aa3facc536f8a922f5	288	0.6728%
16	0x84a0d77c693adabe0ebc48f88b3f010577051	256	0.5981%
17	0x6a7a43be33ba930fe58f34e07d0ad6ba7adb9b1f (Coinotron_3)	241	0.5630%
18	0x4bb96091ee9d802ed039c4d1a5f6216f90f81b01 (Ethpool_2)	229	0.5350%
19	0x4c549990a7ef3fa8784406c1eccc98b4211fa5	198	0.4626%

Figure 3: Miner distribution sorted by blocks mined in Ethereum network over the past 7 days (Data from <https://etherscan.io/> on Oct. 25, 2018 [6])

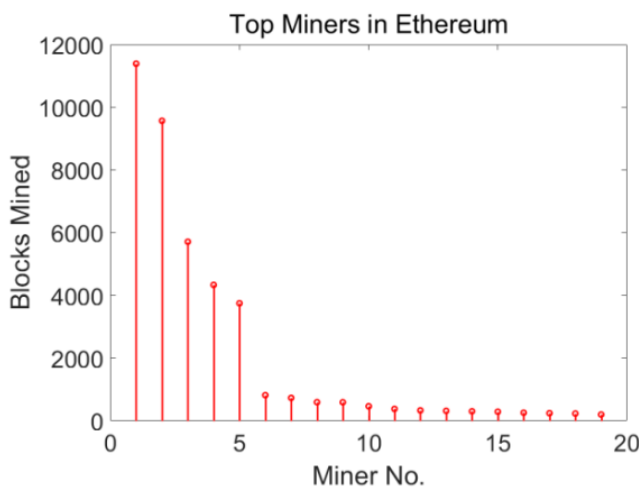


Figure 4: The distribution of top 19 blocks mined in Ethereum network

301, 288, 256, 241, 229, 198} and sample number  $n = 19$  to calculate the coefficient of variation as follows.

$$\mu = \frac{1}{n} \sum_{i=1}^n y_i \approx 2130.11$$

$$\sigma = \sqrt{\frac{1}{n} \sum_{i=1}^n (y_i - \mu)^2} \approx 3271.55$$

$$c_v = \frac{\sigma}{\mu} \approx 1.54.$$

We obtain the value of coefficient of variation of Ethereum blocks mined is approximately equal to 1.54.

## 4.2 Address Balance

This index examines the addresses of the first 100 tokens, and accumulative total tokens as a percentage of the total tokens in the blockchain. We believe that the decentralized blockchain should also decentralize wealth, and the more centralized tokens means that institutions or individuals with a large number of tokens are more likely to manipulate token prices.

### 4.2.1 Coefficient of Variation of Bitcoin Address Balance

We catch the data of Bitcoin address balance (token) from the website [btc.com](http://btc.com) on Oct. 25, 2018 as show in Figure 5.

The green frame in Figure 5 is the data top list of Bitcoin address balances (tokens). The data distribution

#	Address	Balance	Last 30 Days Tx Count	First Tx Time	Last Tx Time
1	3D2oetdNuZUqQHPJmcMDHYoqkyNVsFK9r	133,317.23128155	83	2017-01-05 20:34:15	2018-10-25 02:53:50
2	16ftSEQ4ctQFDtVZ1UBusQUjRrGhM3JYwe	129,234.33723943	19	2017-12-08 15:51:10	2018-10-25 11:39:32
3	16rCmCmbuWdPjWTrpG6aU3EPdZF7MTdUK	107,203.07546044	6	2016-02-28 02:00:09	2018-10-25 11:39:32
4	3Cbq7aT1tY8kxwLbitaG7yT6bPbKChq64	98,042.49937302	8	2017-09-09 00:41:05	2018-10-25 11:39:32
5	3Nkwenay9Z8Lc9JBlywExpnEFLp6Afp8v	97,848.28496144	6	2015-10-16 22:43:06	2018-10-25 11:39:32
6	183hmJGRuTEi2YDCWY5iozY8rZtFwVgahM	85,947.34736772	6	2018-07-01 21:29:21	2018-10-25 11:39:32
7	1FeexV6bAhb8ybZjQMJrCrcrHGw9sb6uF	79,957.19635956	6	2011-03-01 18:26:19	2018-10-25 11:39:32
8	1HQ3Go3ggs8pFnXuVHRytPCq5fG68Hbhx	69,370.12335943	6	2013-04-10 05:03:36	2018-10-25 11:39:32
9	1PnMFRF2ensZnR6J5exxBHuQnxG8Vo5FVK	66,452.07925125	7	2013-11-23 03:06:31	2018-10-25 11:39:32
10	1AhtJUMztC1h1TyA4K6E3QEpbjwLwKhkR	66,378.81086167	6	2014-02-25 13:33:06	2018-10-25 11:39:32
11	1D1hDQMPFu4p84rklN6Majj2LZZRQUaa	66,235.82586355	6	2013-11-23 08:08:37	2018-10-25 11:39:32
12	1EBHA1ckUwzNkN7BmFDwGtx6GKEbADUozX	66,233.75898250	7	2013-11-23 01:05:19	2018-10-25 11:39:32
13	18rnfoGqo1HqvVQaA4QnxjYE75ez9eca	63,600.04702741	20	2014-10-24 18:40:08	2018-10-25 11:39:32
14	34xp4vRoCGJym3xR7yCVPFH0Ckxv4Twiseo	55,482.91464262	28	2018-10-18 20:59:18	2018-10-25 11:39:32
15	1LdRcdxfbSnmCYNdeYpUnzt1YzVfBEQeC	53,880.05876207	6	2014-05-28 06:49:42	2018-10-25 11:39:32
...	...	...	...	...	...
97	1aXzEKIDJkzkPxtZy9zGc3y1nCDwDPubZ	10,900.00003664	5	2016-08-04 18:29:39	2018-10-23 19:50:56
98	332NiYx5Z5CMkULX7ENvcKkxFNCz6Jv5vQ	10,885.20660310	4	2018-07-06 18:17:44	2018-10-23 19:50:56
99	155fzSEBHy9R12bMQ8uuuR3tv1YzcDywd4	10,845.61928398	90	2015-01-28 09:25:06	2018-10-26 04:27:50
100	1F34duy2eelZ5mSrvFepVzy7Y1rBsnAywC	10,770.52537305	3	2011-08-09 06:14:47	2018-10-23 19:50:56

Figure 5: Address Balance in Bitcoin network (Data from <https://btc.com/> on Oct. 25, 2018 [2])

of top 100 address balances (tokens) in Bitcoin network is as show in Figure 6.

Herein we can ignore the decimal digits since the values of address balances are very huge. Therefore, we use the random variable  $X = \{133317, 129234, 107203, 98042, 97848, 85947, 79957, 69370, 66452, 66379, 66236, 66234, 63600, 55483, 53880, 53000, 52431, 51830, 48500, 45899, 40593, 40474, 40438, 40414, 40054, 40000, 36000, 35612, 34010, 32957, 32841, 32796, 32500, 32490, 31925, 31270, 31085, 31000, 30108, 29999, 29772, 29683, 28151, 27833, 27683, 27496, 26215, 25489, 25409, 25403, 25378, 25302, 25272, 25160, 25064, 24000, 23228, 22891, 22211, 22173, 22100, 21603, 20934, 20263, 20008, 20000, 19414, 17955, 17817, 16252, 16224, 16000, 15746, 15500, 15000, 15000, 15000, 14850, 14627, 14500, 14316, 14000, 13900, 13576, 13000, 12800, 12553, 12000, 11927, 11837, 11800, 11337, 11251, 11102, 10960, 10910, 10900, 10885, 10846, 10771\}$  and sample number  $n = 100$  to calculate the coefficient of variation as follows.

$$\mu = \frac{1}{n} \sum_{i=1}^n x_i \approx 32906.88$$

$$\sigma = \sqrt{\frac{1}{n} \sum_{i=1}^n (x_i - \mu)^2} \approx 25055.40$$

$$c_v = \frac{\sigma}{\mu} \approx 0.76.$$

We obtain the value of coefficient of variation of Bitcoin address balances is approximately equal to 0.76.

#### 4.2.2 Coefficient of Variation of Ethereum Address Balance

We also catch the data of Ethereum address balance from the website etherscan.io on Oct. 25, 2018 as show in Figure 7.

The red frame in Figure 7 is the data top list of Ethereum address balances (tokens). The data distribution of top 100 address balances (tokens) in Ethereum network is as show in Figure 8.

Herein we still can ignore the decimal digits since the values of address balances are very huge. Therefore, we use the random variable  $Y = \{1538423, 1510066, 1507810, 1483159, 1378754, 1024185, 1004999, 1000000, 988888, 959123, 825000, 817061, 801053, 672785, 672524, 670941, 658443, 560000, 558117, 552124, 549774, 530000, 505000, 493015, 483000, 450000, 450000, 450000, 436000, 427828, 403085, 395433, 380000, 369023, 365003, 350001, 345741, 325000, 319500, 306276, 281380, 275000, 267786, 254248, 250000, 245342, 245300, 234322, 232419, 221195, 220523, 219824, 207438, 204364, 204176, 203527, 203468, 200782, 195524, 193737, 190905, 190121, 189000, 187068, 185591, 183371, 180001, 176650, 172224, 169032, 166602, 164998, 163197, 150000, 142943, 141354, 137476, 135284, 132930, 132288, 131340, 130379, 130000, 128529, 126850, 125266, 123450, 122862, 121861, 120347, 114939, 113762, 110195, 109488, 109381, 108761, 107866, 107371, 106712, 105114\}$  and sample number  $n = 100$  to calculate the coefficient

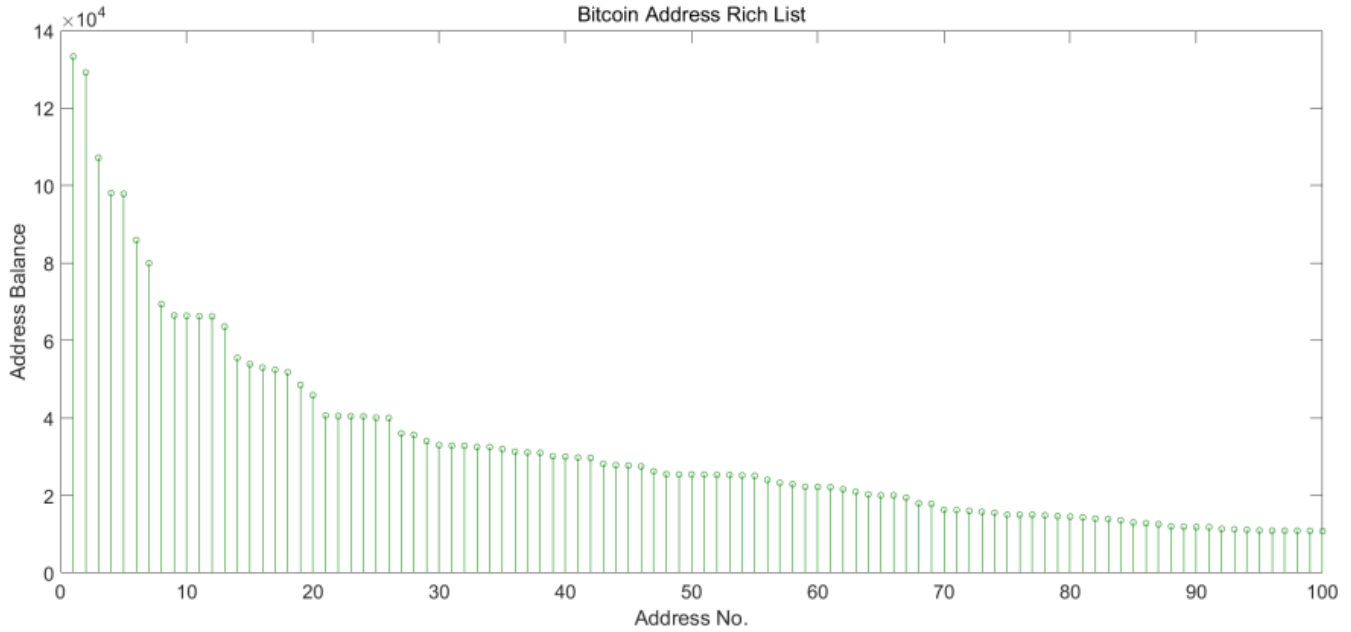


Figure 6: The distribution of top 100 address balance in Bitcoin network

Rank	Address	Balance	Percentage	TxCount
1	0x281055afc982d96fab65b3a49cac8b878184cb16	1,538,423,10656596 Ether	1.49652056%	519
2	0x6f46cf5569aefa1acc1009290c8e043747172d89	1,510,065,64213014 Ether	1.46893548%	499
3	0x90e63c3d53e0ea496845b7a03ec7548b70014a91	1,507,810,43875773 Ether	1.46674170%	446
4	0x742d35cc6634c0532925a3b844bc454e4438f44e	1,483,159,05734310 Ether	1.44276176%	2163
5	0x53d284367ec70ce289d6d64134dfac8e511c8a3d	1,378,754,09306818 Ether	1.34120050%	14994
6	0xc02aaa39b223fe8d0a0e5c4f2ead9083c756cc2	1,024,180,85887157 Ether	0.99628490%	192870
7	0x61edcdf5bb737adffe5043706e7c5bb1fa56eea	1,004,999,00001000 Ether	0.97762550%	118
8	0xab7c74abc0c4d48d1bdad5dc26153fc6780f83e	1,000,000,01146312 Ether	0.97276267%	403
9	0xbe0eb53f46cd790cd13851d5eff43d12404d33e8	988,888,05476810 Ether	0.96195338%	5
10	0xfbb1b73c4f0bda4f67dca266ce6e42f520fbb98	959,169,02268714 Ether	0.93304381%	6966260
11	0xdca70e67b3f93f679992cd36323eeb5a5370c8e4	824,999,89932905 Ether	0.80252910%	36
12	0xdc76cd25977e0a5ae17155770273ad58648900d3	817,060,63884765 Ether	0.79480608%	138
13	0xe853c56864a2ebe4576a807d26fdc4a0ada51919	801,052,79895972 Ether	0.77923425%	147
14	0xd27daf52c38b2c373ad2b9392652dd433303c4	672,784,62216252 Ether	0.65445976%	97
15	0x3d2e397f94e415d7773e72e44d5b5338a99e77d9	672,524,35429759 Ether	0.65420658%	81
...	...	...	...	...
95	0x955a27306f1eb21757ccb8daa2de82675aabc36	109,380,81181740 Ether	0.10640140%	34
96	0x21346283a31a5ad10fa64377e77a8900ac12d469	108,761,24794052 Ether	0.10579871%	38
97	0xe8507b1532fc44e41b48efe45c4abf92c5767c3	107,866,00000000 Ether	0.10492785%	1
98	0x3bc643a841915a267ee067b580bd802a66001c1d	107,371,19229881 Ether	0.10444652%	108
99	0xdb8c6862ea4f5cc843c4b3ed75eb8951714b7635	106,711,69360026 Ether	0.10380498%	1309
100	0x692190b4a5d3524b6fed0465e7400c07d09db954	105,113,55510868 Ether	0.10225038%	28

Figure 7: Address Balances in Ethereum network (Data from <https://etherscan.io/> on Oct. 25, 2018 [7])

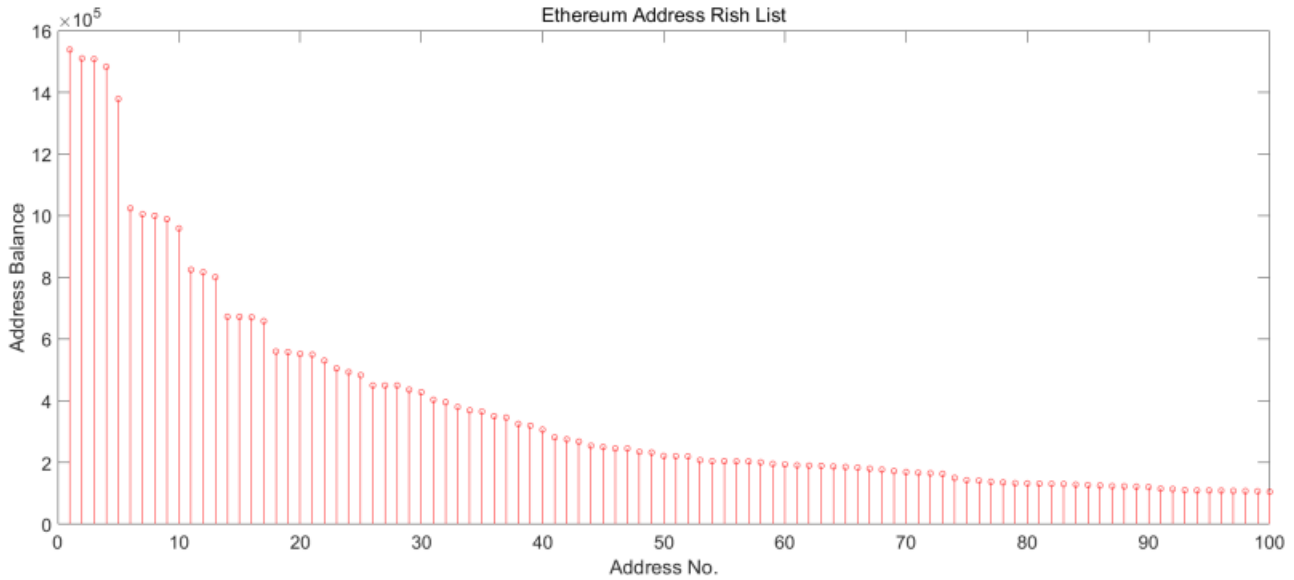


Figure 8: The distribution of top 100 address balances in Ethereum network

of variation as follows.

$$\mu = \frac{1}{n} \sum_{i=1}^n y_i \approx 377230.01$$

$$\sigma = \sqrt{\frac{1}{n} \sum_{i=1}^n (y_i - \mu)^2} \approx 345119.60$$

$$c_v = \frac{\sigma}{\mu} \approx 0.91.$$

We also obtain the value of coefficient of variation of Ethereum address balances is approximately equal to 0.91.

## 5 Comparison and Analysis

We present the comparison of decentralization extents between Bitcoin and Ethereum, and we analyze the centralized and decentralized influences in Bitcoin and Ethereum networks.

### 5.1 Blocks Mined Index

This index examines how many individual or organizational unions are needed to control more than 50% account power. For example, how many pools in PoW will add up to 50% of the total net power. This index intuitively reflects the difficulty of controlling a digital currency through 51% attacks. We believe that the more decentralized the blockchain, the less likely it is to control the entire blockchain by controlling a few individuals or organizations.

According to the results of calculations of coefficients of variation above, the value of coefficient of variation of

Ethereum blocks mined is larger than the value of coefficient of variation of Bitcoin blocks mined, as show in Figure 9.

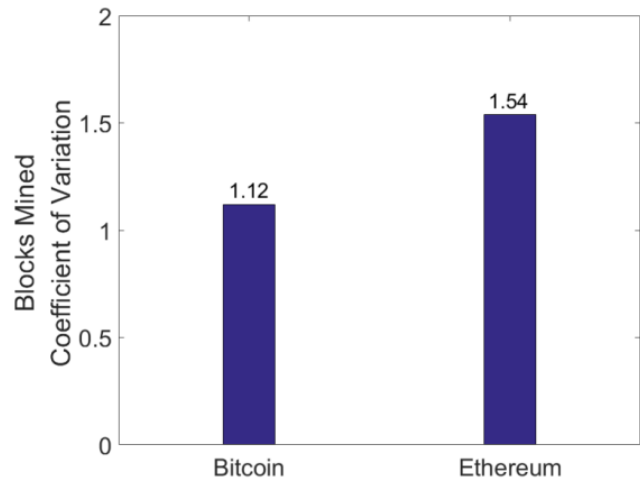


Figure 9: Coefficients of variation of blocks mined comparison between Bitcoin and Ethereum

As shown in Figure 9, Bitcoin mining is more decentralized than Ethereum as measured by blocks mined over the past 7 days. Ethereum mining is somewhat more centralized.

### 5.2 Address Balance Index

This index is a more controversial indicator, because many people would argue that addresses with a large number of tokens may be exchanges. Actually, those tokens are not exchanges, but are temporarily deposited in



exchanges. Herein, we still believe that address balance decentralization is an important factor in the real decentralization of digital money.

According to the results of calculations of coefficients of variation above, the value of coefficient of variation of Ethereum address balance is also larger than the value of coefficient of variation of Bitcoin address balance, as show in Figure 10.

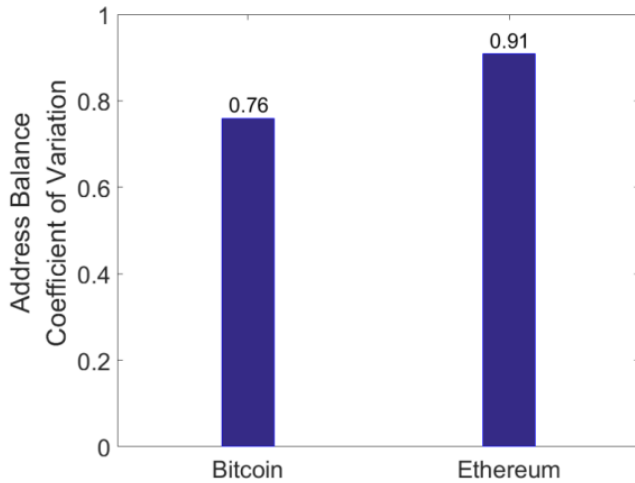


Figure 10: Coefficients of variation of address balances comparison between Bitcoin and Ethereum

As shown in Figure 10, Bitcoin’s wealth is more decentralized than Ethereum as measured by address balances. Ethereum’s wealth is somewhat more centralized.

### 5.3 Extents of Decentralization

To sum up the coefficient of variation results of calculations above, we list the quantitative extents of decentralization for Bitcoin and Ethereum networks as the following table.

Table 1: Extents of decentralization

Coefficient of Variation	Blocks Mined (Top 19)	Address Balance (Top 100)
Bitcoin Network	1.12	0.76
Ethereum Network	1.54	0.91
Comparison (Bitcoin is less than Ethereum)	27.3%	16.5%

This table shows that the extents of decentralization of Bitcoin network are 1.12, 1.54 respectively, and the extents of decentralization of Ethereum network are 0.76, 0.91 respectively. Hence, the extents of decentralization of Bitcoin network are more 27.3%, 16.5% large than Ethereum respectively.

## 6 Conclusions

Decentralization is the most important property of networks like Bitcoin and Ethereum. It is critical to be able to measure the extents of decentralization. More importantly, the coefficient of variation method is one such general measurement method adapting to quantify dispersion for any data set. Therefore, given a proposed blockchain network, we can calculate its coefficient of variation for kinds of targets which you think they are important, and analyze whether this is plausibly a decentralization bottleneck for the network.

## Acknowledgments

This work was supported by the Guangdong Natural Science Foundation (Grant No. 2018A030313746), and the Basic Research Project of Shenzhen (Grant No. JCYJ20170817114239348).

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