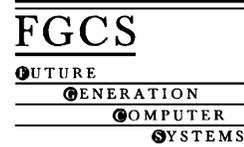




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Future Generation Computer Systems 970 (2003) 1–6



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A new key assignment scheme for enforcing complicated access control policies in hierarchy

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Accepted 10 December 2002

Abstract

In a traditional key assignment scheme, an access control policy is used to solve the access control problem in a hierarchy. A higher security class can access lower security classes, but the opposite is not allowed. However, in some cases, this can be troublesome because of the lack of flexibility. In this paper, we shall propose a secure key assignment scheme which can be performed not only in a hierarchy but also in more complicated policies with anti-symmetrical and transitive exceptions.

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Keywords: Access control; Cryptography; Data security; Key assignment; Multilevel security

1. Introduction

In the past decade, many key assignment schemes have been proposed in the literature to control access in a hierarchy [1–12]. In a hierarchic access control policy, all users are allocated into a number of disjoint sets of security classes C_1, C_2, \dots, C_m . According to the partially ordered hierarchy, a user in security class C_j can derive the secret keys of the users in any security class C_i that is in the same security level as C_j or lower, but the opposite is not allowed. In other words, the users in C_j can access the information held

by the users in C_i . The relation can be expressed as $C_i \leq C_j$.

In real-life situations, many organizations are in partially ordered hierarchies. However, the hierarchy structure is not suitable for all the organization in the societies. For example, there is a more flexible organization structure in Fig. 1. A user in the top level user class C_1 possesses the authority to access information items of classes C_2 and C_4 , but access to the information items of C_3 is not allowed; a user in C_2 can access information items of C_3 and C_4 ; a user in C_4 can access information items of C_2 . It is difficult to meet the relationships by using the traditional key assignment scheme in hierarchy.

Recently, Yeh et al. [14] proposed a more flexible key assignment scheme (named, the YCN scheme) for enforcing access control policy in a user matrix model. The user matrix model cannot only enforce the access control policies in the user hierarchy model

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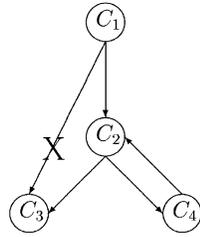


Fig. 1. An example access control policy in a hierarchy structure with explicit anti-symmetric and transitive exceptions.

but also enforce the two extension policies: *transitive exceptions* and *anti-symmetrical arrangements*. The key assignment scheme in the hierarchy structure with an explicit transitive exception policy goes that C_i can access C_j and C_j can access C_k , but C_i cannot access C_k . For example, C_1 can access C_2 and C_2 can access C_3 , but C_1 cannot access C_3 as Fig. 1 shows.

The key assignment scheme in the hierarchy structure with an anti-symmetrical policy is that C_i can access C_j and C_j can access C_i , but C_i and C_j are two different user classes. For example, C_2 can access C_4 and C_4 can access C_2 , but C_2 and C_4 are two different user classes as Fig. 1 shows. Therefore, the YCN scheme is more flexible than the schemes in the user hierarchy model in solving the access control problem. The scheme has opened a brand new research area for key assignment in a hierarchy. However, the YCN scheme is not secure. Hwang presented counter-evidence to point out the YCN scheme is not secure [9]. In some cases, several user classes in YCN scheme can collaborate to derive the derivation and encryption keys. To amend the problem in security, we shall propose a secure key assignment scheme which can also enforce the complicated access control policies. Besides, our proposed scheme does not require large amount of storage for storing the public parameters.

The organization of the paper is as follows. In the next section, we shall briefly review related work on key assignment schemes in a user hierarchy. Following the review, we shall propose our new key assignment scheme for enforcing more flexible access control policies in Section 3. In Section 4, we shall give a simple example to illustrate our scheme. The security of our proposed scheme and the required storage

and computations are analyzed thereafter. Finally, our conclusion will be presented in the last section of this paper.

2. Related work

In this section, we shall introduce some related work on key assignment schemes in a hierarchy. One of the simplest methods to control access in a hierarchy is to make only the authorized users hold all the users' secret keys of the successor security classes. In this simple method, each user must hold and manage a set of subordinate keys. Such an arrangement raises the key management problem of multilevel security [1].

To solve this problem, one of the workable ways is to use a super-key instead of many subordinate keys. The concept of the super-key was first introduced by Akl and Taylor in [1]. Since then, many schemes have been proposed for solving the problem based on the concept of the super-key. Akl and Taylor designed the key assignment scheme using the top-down approach. In their scheme, a central authority (CA) assigns to each user class a prime, a secret key, and a public parameter. If C_j has a security clearance higher than C_i , the users in C_j can easily derive the secret key of C_i with their own secret key and the public parameters of C_i and C_j . Thus, the scheme can solve the key management problem. However, the values of public parameters are very large. Since the public parameter of the user class C_i in the Akl-Taylor scheme is the product of the primes of C_j which is not a descendant of C_i , the scheme requires a large amount of storage to store the public parameters.

In 1985, Mackinnon et al. [11] proposed an algorithm to reduce the values of public parameters in Akl and Taylor's scheme. The method is called canonical assignment. However, the scheme also requires a large amount of storage to store the public parameters [2,12]. Moreover, the optimal canonical algorithm is difficult to find.

In 1990, Harn and Lin [3] proposed a cryptography-based hierarchy scheme. This scheme is similar to the Akl-Taylor scheme, but the Harn-Lin scheme used a bottom-up approach instead of the top-down approach employed in the Akl-Taylor scheme. More-

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129 over, the security of the Harn–Lin scheme is based on
 130 the difficulty of factoring a large number. The main
 131 advantage of this scheme is that the size of the storage
 132 space is much smaller.

133 Recently, many related schemes have been pro-
 134 posed [2,4–7,12]. These schemes are quite advanced
 135 in storage complexity, computational complexity, and
 136 the efficiency of changing the user classes. However,
 137 they are not flexible enough to suit more complicated
 138 policies, such as policies with transitive exceptions
 139 and anti-symmetrical arrangements. In [14], Yeh et al.
 140 proposed a key assignment scheme in a user matrix
 141 model, which is more flexible than the schemes in
 142 a user hierarchy. In the YCN scheme, it is impos-
 143 sible for illegal users to derive the derivation keys
 144 and encryption keys. However, Hwang [9] shown
 145 that several user classes can collaborate to derive the
 146 derivation keys and encryption keys in some cases
 147 under YCN scheme. In this paper, we shall propose
 148 a new key assignment scheme to amend the prob-
 149 lem in security. Our proposed scheme is also more
 150 flexible.

151 3. A new key assignment scheme

152 In this section, we shall propose a new key assign-
 153 ment scheme for access control in a more flexible
 154 hierarchy structure. We design the scheme using the
 155 bottom–up approach. The security of our scheme is
 156 based on the difficulty of factoring a product of two
 157 large primes.

158 There is a CA in our scheme. It is a trust third
 159 party. The responsibility of this CA is to generate and
 160 distribute keys. Initially, CA assigns each user class
 161 two keys: a secret key and a derivation key. The se-
 162 cret key is used to encipher and decipher documents
 163 in a symmetric cryptosystem such as DES, IDEAL, or
 164 AES (advanced encryption standard) [13]. The deriva-
 165 tion key is used to derive the secret key of other
 166 user classes which are allowed to access. The details
 167 of the new key assignment scheme are described as
 168 follows.

169 Step 1 CA randomly chooses two large primes: p and
 170 q . Both of p and q need to be kept secret. Next,
 171 CA calculates n such that $n = p \times q$, where n
 172 is public.

Step 2 CA chooses another parameter, g , which is
 173 relatively prime to n and in the range between
 174 2 and $n - 1$. 175

Step 3 CA chooses a set of distinct primes $\{e_1,$
 176 $e_2, \dots, e_m\}$ for all user classes $\{C_1, C_2, \dots,$
 177 $C_m\}$, where e_i has to relatively prime to
 178 $\phi(n)$, i.e. $\gcd(\phi(n), e_i) = 1$ and $1 < e_i <$
 179 $\phi(n)$. Then, CA publishes the parameters
 180 $\{e_1, e_2, \dots, e_m\}$ and n . 181

Step 4 CA calculates $\{d_1, d_2, \dots, d_m\}$, where each d_i
 182 is the multiplicative inverse of e_i , i.e. $e_i \times d_i \equiv$
 183 $1 \pmod{\phi(n)}$, where $\phi(n)$ denotes the Euler's
 184 totient function of n . 185

Step 5 CA generates the derivation keys $\{DK_1,$
 186 $DK_2, \dots, DK_m\}$ and the secret keys $\{SK_1,$
 187 $SK_2, \dots, SK_m\}$ for all user classes $\{C_1,$
 188 $C_2, \dots, C_m\}$ as follows: 189

$$DK_i = g^{\prod_{C_j < C_i} (d_j)} \pmod{n}, \quad (1) \quad 190$$

$$SK_i = g^{d_i} \pmod{n}. \quad (2) \quad 191$$

$C_j < C_i$ means that the user class C_i pos-
 192 sesses the authority to access the information
 193 items of C_m . Next, CA delivers SK_i and DK_i
 194 to each user in the user class C_i through a se-
 195 cure channel. Each user has to keep SK_i and
 196 DK_i secret. 197

Step 6 If the user classes keep the relation $C_j < C_i$,
 198 an user in class C_i can derive the secret key
 199 of class C_j with the derivation key DK_i as
 200 follows: 201

$$\begin{aligned} SK_j &= DK_i^{\prod_{C_k < C_i, k \neq j} (e_k)} \pmod{n} & 203 \\ &= (g^{\prod_{C_k < C_i} (d_k)})^{\prod_{C_k < C_i, k \neq j} (e_k)} \pmod{n} & 204 \\ &= g^{d_j} \pmod{n}. & (3) \quad 205 \end{aligned}$$

The public parameters in the Akl–Taylor scheme
 206 [1] are the products of the primes associated with
 207 non-authority classes. If there are many user classes
 208 in the system, the values of public parameters will be
 209 very large. Therefore, their scheme requires a large
 210 amount of storage to store the public parameters. In
 211 contrast, the public parameter e_i of user class C_i is
 212 a single prime in our proposed scheme. Thus, our
 213 scheme requires only small storage to store the public
 214 parameters. 215

216 **4. An example**

217 In the following example, we apply the proposed
 218 scheme to the structure of an organization in Fig. 1.
 219 The users in C_1 possess the greatest authority; they
 220 can derive the secret keys of the users in C_2 and C_4 ,
 221 but they cannot derive the secret key of the users in
 222 C_3 because it is restricted by the transitive exceptions
 223 policy. The users in C_2 have the authority to derive the
 224 secret keys of the users in C_3 and C_4 . Furthermore,
 225 the anti-symmetrical policy allows that the users in C_4
 226 can derive the secret key of the users in C_2 . Finally,
 227 the users in C_3 have the least authority; they can only
 228 access information held by the users in the same class
 229 as themselves.

230 Initially, CA chooses the public parameters
 231 e_1, e_2, e_3, e_4 for all user classes C_1, C_2, C_3, C_4
 232 and calculates the public modular n . According to
 233 Eq. (1), CA can calculate the derivation keys $DK_1 =$
 234 $g^{d_2 \times d_4} \bmod n$, $DK_2 = g^{d_3 \times d_4} \bmod n$, $DK_3 = \text{null}$, and
 235 $DK_4 = g^{d_2} \bmod n$ for the users in C_1, C_2, C_3 , and
 236 C_4 , respectively. Obviously, the secret keys $SK_1 =$
 237 $g^{d_1} \bmod n$, $SK_2 = g^{d_2} \bmod n$, $SK_3 = g^{d_3} \bmod n$, and
 238 $SK_4 = g^{d_4} \bmod n$ for the users in C_1, C_2, C_3 , and
 239 C_4 , respectively, can also be calculated by CA using
 240 Eq. (2).

241 Using the derivation keys and the public parameters,
 242 the users in C_1 can derive the secret keys SK_2 and
 243 SK_4 following the equations $SK_2 = DK_1^{e_2} \bmod n$ and
 244 $SK_4 = DK_1^{e_4} \bmod n$, but they cannot obtain the secret
 245 key of C_3 . Similarly, the users in C_2 can also use their
 246 own derivation key to derive the secret keys SK_3 and
 247 SK_4 following the equations $SK_3 = DK_2^{e_3} \bmod n$ and
 248 $SK_4 = DK_2^{e_4} \bmod n$. The users in C_3 cannot derive any
 249 secret key. The secret key of C_3 can also be derived by
 250 the users in C_4 with the equation $SK_2 = DK_4 \bmod n$.
 251 With the secret key, users can decipher the plaintext
 252 and access the information they want. The scheme is
 253 simple, and the access policies are more flexible than
 254 traditional hierarchy structures.

255 **5. Discussions**

256 In this section, we shall examine the security of our
 257 proposed key assignment scheme. In addition, we shall
 258 also discuss the required storage and computational
 259 complexity in our proposed scheme.

5.1. Security analysis

260

261 The security features of our proposed scheme are
 262 described as follows.

- 263 1. *Difficulty for factoring the modular n .* From the
 264 public parameter e_i and the modular n , no one can
 265 derive the multiplicative inverse d_i . The security is
 266 similar to that of the RSA cryptosystem [13]; it is
 267 based on the difficulty of factoring the modular n .
 268 Any adversary who wants to derive the multiplica-
 269 tive inverse d_i from the public parameter e_i and the
 270 modulus n has to factor n into its two prime factors.
 271 Currently, there are many factoring algorithms, but
 272 they are all time-consuming. Furthermore, if an ad-
 273 versary tries all possible corresponding multiplica-
 274 tive inverses, d_i , until he/she finds the correct one,
 275 it is in fact not more efficient than trying to factor
 276 n [13].
- 277 2. *Preventing the unauthorized users to access.* With-
 278 out the authority to access the information in C_j ,
 279 the users in C_i cannot derive the secret key of the
 280 users in C_j . If the users in C_i has the authority
 281 to access the information in C_j , the derivation key
 282 DK_i has a hidden multiplicative inverse d_j . There-
 283 fore, the secret key SK_j will be able to be derived
 284 by Eq. (3). However, if users are not authorized,
 285 the derivation key DK_i will not reveal about C_j ,
 286 and there will be no way for the users to derive the
 287 secret key SK_j from the derivation key DK_i or the
 288 other public parameters.
- 289 3. *Resisting common modulus attack.* If everyone is
 290 given the same modulus n , but different values for
 291 the exponents d_i and e_i , the RSA cryptosystem is
 292 not secure. The problem occurs when the same
 293 message is encrypted by two different exponents
 294 (both having the same modulus), and the two ex-
 295 ponents are relatively prime, then the message can
 296 be recovered without using the private key d_i [13].
 297 The attack is called common modulus attack. For
 298 example, a message m is encrypted by using the
 299 keys e_1 and e_2 . The two ciphertexts are

$$300 \quad c_1 = m^{e_1} \bmod n, \quad \text{and} \quad c_2 = m^{e_2} \bmod n.$$

301 Since the e_1 and e_2 are relatively prime, we can
 302 derive r and s using Euclidean algorithm, such that

$$303 \quad re_1 + se_2 = 1.$$

Thus, the plaintext m can be recovered by using the following equation without the private key d :

$$(c_1)^r \times (c_2)^s = m \bmod n.$$

In our scheme, even though all user classes use the same modulus and different values for the exponents e and d , our system will not reveal any information under the common modulus attack. Since $SK_i = g^{d_i} \bmod n$ must be kept secret by the users in class C_i , no public parameters are calculated by power of e_i modular n . Even through several users reveal their secret keys SK_i in different user classes C_i , only the parameter g can be derived by using the common modulus attack. However, revealing the parameter g does not harm the security of our scheme, because the multiplicative inverses d_i are unknown.

4. *Resisting collaborate attack.* In collaborate attack, several user classes may reveal their derivation keys and secret keys to try to derive the derivation keys and secret keys of the unauthorized classes. Using the common modulus attack with the revealed secret keys, only the parameter g can be derived. Furthermore, the exponential of $DK_i = g^{\prod_{C_j < C_i} (d_j)} \bmod n$ only contains the multiplicative inverses d_j of the authorized classes. Therefore, the collaboration is not helpful to derive the derivation keys and secret keys of the unauthorized classes. The key pointer is that the multiplicative inverses d_i are unknown, they are kept secret by CA.

5.2. Required storage and computational complexity

Assume that there are m user classes in the hierarchy. From the algorithm of our proposed scheme, the public parameters $\{e_1, e_2, \dots, e_m\}$ and n are $m + 1$ integers, where the binary value of $\{e_1, e_2, \dots, e_m\}$ are between 1 and $\phi(n)$. That is, the size of the public parameters must be less than or equal to $\log_2(n)$. Let the size of each public parameter is k bits, where $2^{k-1} < n \leq 2^k$. Generally, the length of k in the range of 512–1024 bits is secure [13]. Therefore, the amount of the required storage for storing the public parameters is $(m + 1) \lceil \log_2(n) \rceil$ bits, i.e. $(m + 1)k$ bits. Recalling the Akl–Taylor scheme, the public parameter of the user class C_i is a product of the primes dedicated to the user classes which are not the descendants of C_i . Obviously, the amount of the required storage in

our scheme is much less than the Akl–Taylor scheme, especially when the number of user classes in the hierarchy is large.

The computational complexity of our scheme is also simple. When a user in class C_i and the relationship $C_j < C_i$ holds, the user can derive the secret key of class C_j with the derivation key DK_i from Eq. (3). It requires r multiplications and 1 modular exponential computations, where r is the number of immediate successors of the processed user class. Therefore, our scheme is efficient to implement.

6. Conclusions

We have proposed a secure key assignment scheme for solving the multilevel access control problem in complicated access control policies. The main contribution of our scheme is that it can be used in more flexible applications than that of the scheme proposed before. In this scheme, the access control policy not only able to be enforced in a hierarchy but also able to be employed for more complicated policies with anti-symmetrical arrangements and transitive exceptions. Furthermore, our scheme does not require large amount of storage for storing public parameters.

Acknowledgements

The authors wish to thank many anonymous referees for their suggestions to improve this paper. This research was partially supported by the National Science Council, Taiwan, ROC, under contract no.: NSC91-2213-E-324-003.

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