

# An Image Authentication Scheme Based On Digital Signatures \*

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## Abstract

It is important to protect digital pictures and detect tampered image locations in digital Cyberspace. In this paper, we propose an image authentication scheme based on digital signatures. The proposed scheme is capable of detecting if certain blocks of an image have been altered. The block can be as small as 86 image pixels.

*Keywords:* Authentication, Cryptography, Digital signature, Image authentication.

## 1 INTRODUCTION

It is necessary to protect digital media because information such as images; audio/video data, text, and software are transmitted via the Internet. Consider the following case. When an image is used as a piece of evidence in the prosecution of a crime, the court must make sure that the evidence has not been altered. Without this guarantee, the image can not be used as legal evidence. Such an image can be a matter of life and death in a criminal case. The ability to accurately verify the authenticity of an image, as well as detecting the altered locations in a tampered image is extremely important. When an image is transferred over the network, hackers may intercept it and make changes to it. Similarly, an image file produced by a digital camera [2] may be doctored for certain purposes.

Recently, many approaches [2, 6, 7] have been proposed to solve the problem of image authentication, including the legal use of images and trusted camera and medical image archiving. In these methods, the owner or receiver of the image must have a priori knowledge about the image size [6] or its look-up table [7]. For example, Wong proposed a public key watermark [6] for image

verification and authentication. This approach can not only authenticate an image, but also identify the tampered location. However, one of the drawbacks is that the smallest detectable block is 172 pixels. It is thus desirable to develop a scheme that can effectively detect altered blocks smaller than 172 pixels. In this paper, we introduce a new method for image authentication, which is able to detect an altered image block as small as 86 pixels.

An effective authentication and verification scheme should have the following features:

- Determine if the image or data has been modified.
- Enable a defense for any attack.
- Be independent from the image size or the look-up table.

Our method used the RSA cryptosystem to generate and put a signature into the least significant bits (LSB) of each block. This scheme can be applied to a "secure" digital camera [2] for authenticating and detecting altered image pixels.

This paper is organized as follows. Section 2 introduces the basic idea of how to encrypt image blocks into LSB. Section 3 provides some experimental results. The analysis is performed in section 4, and section 5 gives the concluding remarks.

## **2 OUR SCHEME**

The main idea of our method is to perform set operations to detect altered blocks. Our scheme is based on the RSA signature with 512 bits [1]. Five hundred and twelve bits are used for protecting each image block. This method can detect altered locations as sub-blocks. The following discussions are focused on gray level images. For color images, the same technique applies.

Let  $I_{mn}$  be a gray level image of size  $m$  by  $n$  pixels. The most significant bits (MSB) and least significant bits (LSB) of each pixel in our scheme are 5 and 3 bits, respectively. Since each signature block is 512 bits in the RSA cryptosystem, we require 172 pixels (as a block) to input a signature. The total number of MSBs and LSBs in a block (172 pixels) are 860 and 516 bits, respectively. In a straightforward method, we can hash the 860 bits (an MSB block) to 516 bits. A signature can then be made with 516 bits and placed into the LSB block using the RSA cryptosystem. If the block has not been altered, the MSBs of the signature will be equal to the LSBs. If the MSB of the signature are not equal to the LSBs, we can be certain that a portion of this block has been altered. This straightforward method only can determine if the block (172 pixels) has been altered. In this section, we will propose a method that can reduce the detectable size to 86 pixels. This method consists of 6 steps as follows.

**Step 1: Collect and construct the first block.**

According to the RSA standard, at least 512 bits are necessary for an encryption to effectively resist any attack. Because the LSB is defined as 3 bits/pixel, 172 pixels must be collected to form a signature ( $172 \times 3 = 516$  bits). Now every first 5 bits (MSB) of the 172 pixels are collected to form the block  $b_1$ , which represents the image data. The final 3 bits (LSB) of each pixel are collected to form  $w_1$ , i.e. the signature. In our method,  $b_1$  is further divided into two 86 pixel sub-blocks, denoted  $sb_1$  and  $sb_2$ , as shown in Figure 1, and then all bits in  $w_1$  are set to zero. The block with the signature structure is illustrated in Figure 2(a).

**Step 2: Second stage block collection and construction.** In this

Figure 1: Blocks with MSBs and LSBs structure.

Figure 2: Blocks with signature  $S_i$  structure. Here,  $H(b_i) = Hb_i$  and  $S_i = E_d(Hb_i), i = 1, 2, \dots, r$ .

Figure 3: Embedding a signature into an image.

step, we denote the second to the last block as  $b_2$  to  $b_r$ , respectively, where  $r = \lceil \frac{m \times n}{172} \rceil$ . Every block  $b_r$  is divided into three sub-blocks ( $sb_{2(r-1)}$ ,  $sb_{2r-1}$ ,  $sb_{2r}$ ). An example of blocks with a signature structure is shown in Figures 1 and 2(b). The steps for embedding a signature into an image are shown in Figure 3.

In the previous steps, 1 and 2, the block  $b_1 = sb_1 + sb_2$ ,  $b_2 = sb_2 + sb_3 + sb_4$ ,  $\dots$ ,  $b_r = sb_{2(r-1)} + sb_{2r-1} + \dots + sb_{2r}$ , where  $+$  denotes concatenation. Since, the size of sub-block  $sb_i$  is equal to 86 pixels, the number of pixels in  $b_1$  is 172 and the number of pixels in the others  $b_i$ ,  $i = 2, \dots, r$ , are equal to 258.

**Step 3: One-way hash function process.** Let  $H$  be a one-way hash function, such as MD5 [3].  $H$  can be formulated as:

$$H(b_i) = Hb_i, i = 1, 2, \dots, r. \quad (1)$$

Here, the length of  $b_1$  is 860 bits ( $= 172 \times 5$ ); The lengths of  $b_i$ ,  $2 \leq i \leq r$ , are 1290 bits ( $= 258 \times 5$ ); The lengths of  $Hb_i$ ,  $i = 1, 2, \dots, r$ , are 516 bits.

**Step 4: Generating and embedding the signature.** The RSA cryptosystem is used to generate the digital signature  $S_i$  as follows.

$$S_i = E_d(Hb_i), i = 1, 2, \dots, r. \quad (2)$$

Here,  $d$  denotes the system's private key.  $E$  denotes the RSA algorithm [4] with 516 bits. The length of  $S_i$  is 516 bits. The signatures  $S_i$  are embedded into  $w_i$ ,  $i = 1, 2, \dots, r$ .

Figure 4: Extracting a signature from a protected image.

**Step 5: Image authentication.** When an image is received, it is necessary to perform an authentication process and determine if and where the image has been altered. The authentication process consists of 6 consecutive tasks as delineated in Figure 4. The first three tasks are the same as in Step 1. i.e., the hash values  $HB'_i$ ,  $i = 1, 2, \dots, r$  are obtained. The fourth task uses the RSA cryptosystem [4] to recover the signature  $S_i$  as follows.

$$Dhb_i = D_e(S_i), i = 1, 2, \dots, r. \quad (3)$$

Here,  $e$  denotes the system's public key.  $D$  denotes the RSA deciphering algorithm. If the image has not been altered, each pair of  $Hb'_i$  and  $Dhb_i$  should match. Otherwise, the image has been altered.

**Step 6: Identify the tampered location.** If one or more pairs  $Hb'_i$  and  $Dhb_i$  do not match, we know that the image has been altered. In this step, we propose a method to locate the altered location within the range of 86 pixels. The following rule is used to confine the altered location. We define three sets as follows.

- $A = \{sb_i | \text{a set of the pairs } Hb'_i \text{ and } Dhb_i \text{ do not match.}\}$ .

- $B = \{sb_j | \text{a set of the pairs } Hb'_j \text{ and } DHB'_j \text{ match.}\}$ .
- $C = \{sb_k | \text{a set of probable altered sub-blocks.}\}$ . In other words,  $C = A - B$ . Here,  $-$  denotes a difference set operation.

For example, if all  $Hb'_i$  and  $DHB'_i$  match except for  $Hb'_2$  and  $DHB'_2$ , we know that the block  $b_2$  has been altered. By our rule,  $A = \{sb_2, sb_3, sb_4\}$ ,  $B = \{sb_1, sb_2, sb_4, sb_5, \dots\}$ , and,  $C = A - B = \{sb_3\}$ . Therefore, we obtain a probable altered sub-block  $sb_3$ . This means that the altered locations can be detected at a range of 86 pixels.

### 3 EXPERIMENTAL RESULTS

The experimental result is shown in Figure 5. We used the "Lena" image ( $256 \times 256$  pixels) as the test image. Figure 5(a) is an original image. Figure 5(b) is an image with a signature embedded into the original image. Figure 5(c) is an image with a black eyeball that has been altered. Figure 5(d) is a detection image using our scheme. Where the image color is black denotes that this location has not been altered. The other color denotes a location that has probably been altered. In this experimental result, the length of the tampered area is 86 pixels.

### 4 ANALYSIS

Some tampered image cases are analyzed in this section. The sub-blocks in shadow denote that these sub-blocks have been altered.

#### Case 1: Sub-block $sb_1$ is altered (shown in Figure 6).

Block  $b_1$  does not match in Step 5 of Section 2, while  $b_2$ ,  $b_3$ , and other blocks do match. Using our method in Step 6 of Section 2,

Figure 5: Experimental result

Figure 6: Case 1: a sub-block is altered.

- $A = \{sb_1, sb_2\}$ .
- $B = \{sb_2, sb_3, sb_4, \dots, sb_r\}$ .

The probable tampered sub-block is  $C = A - B = \{sb_1\}$ .

In the straightforward method (described in Section 2), the detected tampered sub-blocks are  $sb_1$  and  $sb_2$ . The length of detected tampered pixels is 172 pixels. However, the length of the detected tampered pixels is only 86 pixels using our method.

**Case 2: Sub-block  $sb_1$  and  $sb_2$  are altered (shown in Figure 7).**

Blocks  $b_1$  and  $b_2$  do not match in Step 5 of Section 2, while  $b_3$  and other blocks do match. Using our method in Step 6 of Section 2,

- $A = \{sb_1, sb_2, sb_3, sb_4\}$ .
- $B = \{sb_4, sb_5, sb_6, \dots, sb_r\}$ .

Figure 7: Case 2: Two sub-blocks in a block are altered.

The probable tampered sub-block is  $C = A - B = \{sb_1, sb_2, sb_3\}$ .

In the straightforward method (described in Section 2), the detected tampered sub-blocks are  $sb_1$  and  $sb_2$ . The length of detected tampered pixels is 172 pixels. However, the length of the detected tampered pixels is 258 pixels using our method. We conclude that if two sub-blocks in a block are altered, then the straightforward method is better than our method.

**Case 3: Sub-blocks  $sb_2$ , and  $sb_3$  are altered (shown in Figure 8).**

Blocks  $b_1$  and  $b_2$  do not match in Step 5 of Section 2, while  $b_3$  and other blocks do match. Using our method in Step 6 of Section 2,

- $A = \{sb_1, sb_2, sb_3, sb_4\}$ .
- $B = \{sb_4, sb_5, sb_6, \dots, sb_r\}$ .

The probable tampered sub-block is  $C = A - B = \{sb_1, sb_2, sb_3\}$ .

In the straightforward method (described in Section 2), the detected tampered sub-blocks are  $sb_1$ ,  $sb_2$ ,  $sb_3$ , and  $sb_4$ . The length of detected tampered pixels is 344 pixels. However, the length of the detected tampered pixels is 258 pixels using our method. We conclude that if two consecutive sub-blocks  $sb_{2i}$  and  $sb_{2i+1}$  in different blocks  $b_i$  and  $b_{i+1}$ , respectively, are altered, then our method is better than the straightforward method.

**Case 4: Sub-block  $b_2$  is altered (shown in Figure 9).**

Figure 8: Case 3: Sub-blocks  $sb_2$  and  $sb_3$  are altered.

Figure 9: Case 4: Sub-block  $b_2$  is altered.

Blocks  $b_1$  and  $b_2$  do not match in Step 5 of Section 2, while  $b_3$  and other blocks do match. Using our method in Step 6 of Section 2,

- $A = \{sb_1, sb_2, sb_3, sb_4\}$ .
- $B = \{sb_4, sb_5, sb_6, \dots, sb_r\}$ .

The probable tampered sub-block is  $C = A - B = \{sb_1, sb_2, sb_3\}$ .

In the straightforward method (described in Section 2), the detected tampered sub-blocks are  $sb_1$  and  $sb_2$ . The length of detected tampered pixels is 172 pixels. However, the length of the detected tampered pixels is 258 pixels using our method. We conclude that if a sub-block  $sb_{2i}$  in a block  $b_i$  is tampered, then the straightforward method is better than our method.

**Case 5: Sub-block  $sb_3$  is altered (shown in Figure 10).**

Block  $b_2$  does not match in Step 5 of Section 2, while  $b_1$ ,  $b_3$ , and other blocks do match. Using our method in Step 6 of Section 2,

Figure 10: Case 5: Sub-block  $sb_3$  is altered.

- $A = \{sb_2, sb_3, sb_4\}$ .
- $B = \{sb_1, sb_2, sb_4, sb_5, sb_6, \dots, sb_r\}$ .

The probable tampered sub-block is  $C = A - B = \{sb_3\}$ .

In the straightforward method (described in Section 2), the detected tampered sub-blocks are  $sb_3$  and  $sb_4$ . The length of detected tampered pixels is 172 pixels. However, the length of the detected tampered pixels is 86 pixels using our method. We conclude that if a sub-block  $sb_{2i-1}$  in a block  $b_i$  is altered, then our method is better than the straightforward method.

Although, our method is not better the straightforward method in some cases, the main merit of our scheme is that our scheme can detect a tampered location within 86 pixels.

## 5 CONCLUSIONS

In this paper, we have presented a new method for image authentication, which can detect a tampered block with size as small as 86 image pixels. In addition, this method has the following features:

- A prior knowledge is not necessary for detecting tampering in an image.
- Any method that an attacker uses to tamper with an image is detectable by our scheme.

## References

- [1] D. Atkins, M. Graff, A. K. Lenstra, and P. C. Leyland. The magic words are squeamish ossifrage. *In Advance in Cryptology, Asiacrypt '94*, pages 263–277, 1994.
- [2] G. L. Friedman. The trustworthy digital camera: Restoring credibility to the photographic image. *IEEE Trans. On Consumer Electronic*, 1993.
- [3] R. L. Rivest. The md5 message digest algorithm. *Internet RFC 1321*, April 1992.
- [4] R. L. Rivest, A. Shamir, L. Adleman, and P. C. A method for obtaining digital signatures and public-key cryptosystems. *Communications of the ACM*, 21:120–126, February 1978.
- [5] Bruce schneier. *Applied Cryptography*. Proc. IEEE Intl. Conf. On Image Processing, second ed edition, 1996.
- [6] P.W. Wong. A public key watermark for image verification and authentication. *Proc. IEEE Intl. Conf. On Image Processing*, pages 455–459, Oct 1998.
- [7] M. Wu and B. Liu. Watermarking for image authentication. *Proc. IEEE Intl. Conf. On Image Processing*, pages 437–441, Oct 1998.