

# A Flexible Remote User Authentication Scheme Using Smart Cards

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## Abstract

In 1999, Hwang and Li proposed a new user authentication scheme using smart cards. The scheme does not need any password or verification table. Later, Sun proposed an efficient remote use authentication scheme to improve the efficiency of the Hwang-Li scheme. However, these two schemes do not allow users to freely choose and change their passwords. In this article, we shall propose a simple and efficient remote user authentication scheme that allows users to freely choose and change their passwords without significantly increasing the computation cost.

*Keywords:* Authentication, cryptography, password, security.

## I Introduction

Recently, based on various techniques, many password authentication schemes using smart cards have been proposed by some researchers [1, 2, 3, 6, 9, 10]. These schemes can allow a legal user to login to remote server and the legal user will be granted access to the server's facilities. Based on ElGamal's cryptosystem [4], Chang and Liao proposed a remote password authentication scheme [1]. However, this scheme has a weakness that users cannot freely choose and change their passwords. Based on Chinese Remainder Theorem (CRT), Chang and Wu proposed a remote password authentication scheme [2]. Based on geometric Euclidean plane, Wu proposed a new remote login authentication scheme [10]. Its simplicity of geometry and the property allow users can freely choose their own passwords. However, this scheme is attacked by Hwang [5]. And in [3], Chien et al. proposed another attack to Wu's scheme and remedy his scheme.

Based on ElGamal's cryptosystem, Hwang and Li proposed a remote user authentication scheme using smart cards [6]. The scheme does not need any password and verification table for authentication. Later, Sun proposed an efficient remote use authentication scheme using smart cards [9]. He claimed that his scheme was much more efficient than Hwang and Li's scheme. However, in these two schemes, the users are not allowed to freely choose and change their passwords which can be a major drawback. Hence, in this paper, we shall propose a new scheme that allows users to freely choose and change their passwords without significantly increasing the computation cost.

This paper is organized as follows. We shall first review the Hwang-Li's scheme and the Sun's scheme in Section 2. Then, in Section 3, we shall propose a simple and efficient

remote user authentication scheme. In Section 4, we analyze the security of our scheme. In Section 5, we show its efficiency. Finally, a brief conclusion will be given in Section 6.

## II Literature Reviews

In this section, we briefly review the Hwang-Li's scheme [6] and the Sun's scheme [9]. Each of these two schemes is composed of three phases: the registration phase, the login phase, and the authentication phase.

### 2.1 The Hwang-Li's Scheme

#### Registration Phase:

The main task of this phase is to deliver a smart card to each registered user. When a user  $U_i$  wants to register with the server,  $U_i$  first submits his/her identity  $ID_i$  to the server. Then the server computes  $PW_i$  for  $U_i$  as follows:

$$PW_i = ID_i^{x_s} \bmod P. \quad (1)$$

Here  $x_s$  is a secret key for the server, and  $P$  is a large prime number of 1024 bits. Then the registration center stores  $PW_i$ , one-way function  $h$ , and  $P$  into the smart card. The smart card is delivered to the user by the registration center.

#### Login Phase:

To log in the system and access the resources,  $U_i$  first inserts his/her own smart card and keys in his/her  $(ID_i, PW_i)$ . Afterwards, the smart card will perform the following tasks:

1. Randomly choose an integer  $r$ .
2. Calculate  $C_1 = ID_i^r \bmod P$ .
3. Calculate  $t = h(T \oplus PW_i) \bmod (P - 1)$ , where  $T$  is the current date and time, and  $\oplus$  denotes an exclusive operation.
4. Calculate  $M = ID_i^t \bmod P$ .
5. Calculate  $C_2 = M(PW_i)^r \bmod P$ .
6. Send the messages  $C = (ID_i, C_1, C_2, T)$  to the server.

#### Authentication Phase:

After receiving the message  $C$  from  $U_i$ , the server verifies the login user as follows:

1. Check the validity of  $ID_i$ . If it is incorrect, then the server rejects the login user  $U_i$ .
2. Check the time interval between  $T$  and  $T'$ , where  $T'$  is the moment when the server receives the message from  $U_i$ . If  $(T' - T) \geq \Delta T$ , then the server rejects  $U_i$ . The time interval  $\Delta T$  denotes the expected legal time interval for transmission delay.
3. Calculate  $PW_i = ID_i^{x_s} \bmod P$  and  $t = h(T \oplus PW_i) \bmod (P - 1)$ . Then check the following equation:

$$C_2(C_1^{x_s})^{-1} \bmod P = ID_i^t \bmod P. \quad (2)$$

If the above equation holds, the login user  $U_i$  is verified and is permitted to access the server.

In Hwang and Li's scheme, this scheme has much computation cost. It is inefficiency. Therefore, Sun proposed an efficient improvement of Hwang-Li scheme. The Sun's scheme is shown as the next subsection.

## 2.2 The Sun's Scheme

### Registration Phase:

The registration phase in Sun's scheme is similar to that in the Hwang-Li scheme. However, there are two differences: One is Sun assumes that  $h$  is a one-way function with an output of 64 bits, and the other is

$$PW_i = h(ID_i, x_s). \quad (3)$$

### Login Phase:

After a user keys in his/her  $ID_i$  and  $PW_i$ , the smart card will perform the following tasks:

1. Calculate  $C_1 = h(T \oplus PW_i)$ , where  $T$  is the current date and time by the input device.
2. Send the message  $C = (ID_i, C_1, T)$  to the server.

### Authentication Phase:

After receiving the message  $C$  from  $U_i$ , the server verifies the login user as follows:

1. Steps 1 and 2 are the same as those in the Hwang-Li's scheme.
2. Calculate  $PW_i = h(ID_i, x_s)$  and  $C'_1 = h(T \oplus PW_i)$ . Then compare  $C_1$  with  $C'_1$ ; if they match, the login user  $U_i$  is verified and is permitted access the server.

Since the Sun's scheme only uses one-way hash function, it reduces much more computation cost in Hwang-Li scheme. Therefore, this scheme is much more efficient than Hwang and Li's scheme. However, Hwang-Li scheme and Sun's scheme have the same weakness that the users are not allowed to freely choose and change their passwords. In this paper, we propose a new scheme to remedy it in the following section.

## III Our Scheme

In this section, we shall depict our new simple, efficient remote user authentication scheme using smart cards. Unlike the Hwang-Li's scheme and Sun's scheme, our new scheme allows users to freely choose and change their passwords. In addition, the security is also based on one-way function, which is the same as Sun's scheme.

### Registration Phase:

This phase is completed by the registration center, whose main task is to deliver a smart card to each registered user. When a user  $U_i$  wants to register with the server,  $U_i$  first chooses his/her own password  $PW_i$  and then computes  $h(PW_i)$ , where  $h$  is a one-way function with an output of 64 bits. The user  $U_i$  submits his/her  $ID_i$  and  $h(PW_i)$  to the server. Then the server computes  $PW_{1i}$  for  $U_i$  as follows:

$$PW_{1i} = h(ID_i \oplus x_s) \oplus h(PW_i). \quad (4)$$

Here  $x_s$  is a secret key for the server; and  $\oplus$  denotes an exclusive operation. Then, the registration center stores  $PW_{1i}$  and  $h$  into the smart card. Finally, the smart card is delivered to the user by the registration center.

### Login Phase:

To log in the server and access the resources,  $U_i$  first inserts his/her own smart card and keys in his/her  $(ID_i, PW_i)$ . Afterwards, the smart card will perform the following tasks:

1. Calculate  $PW_{2i} (= PW_{1i} \oplus h(PW_i) = h(ID_i \oplus x_s))$ .
2. Calculate  $C_1 = h(PW_{2i} \oplus T)$ , where  $T$  is the current date and time.
3. Send the message  $C = (ID_i, C_1, T)$  to the server.

Note that, in order to reduce computational cost,  $h(PW_i)$  can be pre-computed and stored in the smart card.

**Authentication Phase:**

Upon receiving the message  $C$  from  $U_i$ , the server verifies the login user as follows:

1. Check the validity of  $ID_i$ . If it is incorrect, then the server rejects the login user  $U_i$ .
2. Check the time interval between  $T$  and  $T'$ , where  $T'$  is the time when the server receives the message from  $U_i$ . If  $(T' - T) \geq \Delta T$ , then the server rejects  $U_i$ . Here,  $\Delta T$  denotes the expected legal time interval for transmission delay.
3. Check the equation

$$C_1 = h(h(ID_i \oplus x_s) \oplus T). \quad (5)$$

If the above equation holds, the login user  $U_i$  is verified and is permitted access the server.

If the remote user wants to change his/her password, he/she only has to perform the procedures below:

1. Calculate  $PW_{1i} \oplus h(PW_i) = h(ID_i \oplus x_s)$ .
2. Select his/her new password  $PW'_i$  and then calculate  $h(PW'_i)$ .
3. Calculate  $PW'_{1i} (= h(ID_i \oplus x_s) \oplus h(PW'_i))$ .
4. Store  $PW'_{1i}$  into his/her smart card in place of  $PW_{1i}$ .

In our scheme, we only use one-way hash function. It also reduces much more computation cost in Hwang-Li scheme. Furthermore, our new scheme allows users to freely choose and change their passwords to remedy the weakness of Hwang-Li and Sun's scheme.

## IV Security Analysis

In this section, we analyze the security of our scheme as follows.

1. Due to the fact that the one-way function is computationally difficult to invert, it is extremely hard for the user  $U_i$  to derive the secret key  $x_s$  of the server from Equation (4). Even if the smart card of the  $U_i$  is picked up by an intruder, it is also difficult for the intruder to derive the  $x_s$ .
2. No one can forge a valid  $C = (ID_i, C_1, T)$  because  $C_1 (= h(PW_{2i} \oplus T))$  can only be derived from  $PW_i$  and  $x_s$ .
3. The added time-stamp  $T$  prevents the replay attack. With the time-stamp, the system can check the correct time frame and prevent an intruder from replaying messages. To pass the authentication phase, an intruder must somehow change his/her  $T$  to match the requirement  $(T' - T) \geq \Delta T$ . However, if  $T$  is changed, Step 3 in the authentication phase cannot be passed unless  $C_1$  has also been changed and  $x_s$  is known to the intruder, both of which seem out of the question.
4. In cases where a smart card is lost, no one can impersonate the smart card owner to login the server. The intruder will not know the user's password  $PW_i$ , and therefore he/she cannot compute  $PW_{2i}$ . The intruder cannot pass the authentication phase successfully. In addition, if an intruder (who picks up the smart card) only knows  $PW_{1i}$ ; he/she still cannot derive  $x_s$  and  $PW_i$ .

In our scheme, we suppose the one-way function is secure. This function,  $h : x \rightarrow y$ , has the four properties [7, 8]. First, The function  $h$  can take a message of arbitrary-length input and produce a message digest of a fixed-length output. Second, since the function  $h$  is one-way, it is easy to compute  $h(x) = y$  when given  $x$ . However, given  $y$ , it is hard to compute  $h^{-1}(y) = x$ . Third, The function  $h$ , given  $x$ , it is computationally infeasible to find  $x' \neq x$  such that  $h(x') = h(x)$ . Fourth, The function  $h$ , it is computationally infeasible to find any two pair  $x$  and  $x'$  such that  $x' \neq x$  and  $h(x') = h(x)$ .

## V Efficiency

In this section, we compare Hwang-Li's scheme, Sun's scheme, and our scheme in terms of efficiency. In Hwang-Li's scheme, the security is based on the discrete logarithm problem, and  $P$  is as large as 1024 bits to make the puzzle unbreakable. In Sun's scheme and our scheme, on the other hand, the security is based on the one-way function with an output of 64 bits.

In Table 1, we list the efficiency comparison of Hwang-Li's scheme, Sun's scheme, and our scheme. It can be seen that Sun's scheme and our scheme are more efficient than Hwang-Li's scheme. And our scheme consumes one more hashing than Sun's scheme, computationally speaking, in the registration phase. However, our scheme can support users to freely choose and change their passwords.

Table 1: Comparison among Hwang-Li's scheme, Sun's scheme, and our scheme

	Hwang-Li's Scheme	Sun's Scheme	Our Scheme
Length of Password	1024 bits	64 bits	64 bits
Length of Transmitting in Login Phase*	2048 bits	64 bits	64 bits
Computations in Registration Phase	$1 T_{Exp}$	$1 T_H$	$2 T_H$
Computations in Login Phase	$3 T_{Exp} + 1 T_H$	$1 T_H$	$1 T_H$
Computations in Authentication Phase	$3 T_{Exp} + 1 T_H$	$2 T_H$	$2 T_H$
Computations in Change Password Phase	Not supported	Not supported	$2 T_H$
Public Information in Smart Card	(h, P)	h	h

\*The non-cryptographic parameters  $ID_i$  and  $T$  are excluded from reckoning;  $T_{Exp}$  denotes a time to compute an exponential operation;  $T_H$  denotes a time to compute a one-way hash function.

## VI Conclusions

In this article, we have proposed a simple and efficient remote user authentication scheme. Compared with our scheme, the Hwang-Li's scheme and Sun's scheme are not practical enough because they do not allow users to freely choose and change their passwords. The

proposed scheme has succeeded in allowing a user to freely change and choose his/her password without significantly increasing the computation cost.

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## BIOGRAPHY

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